

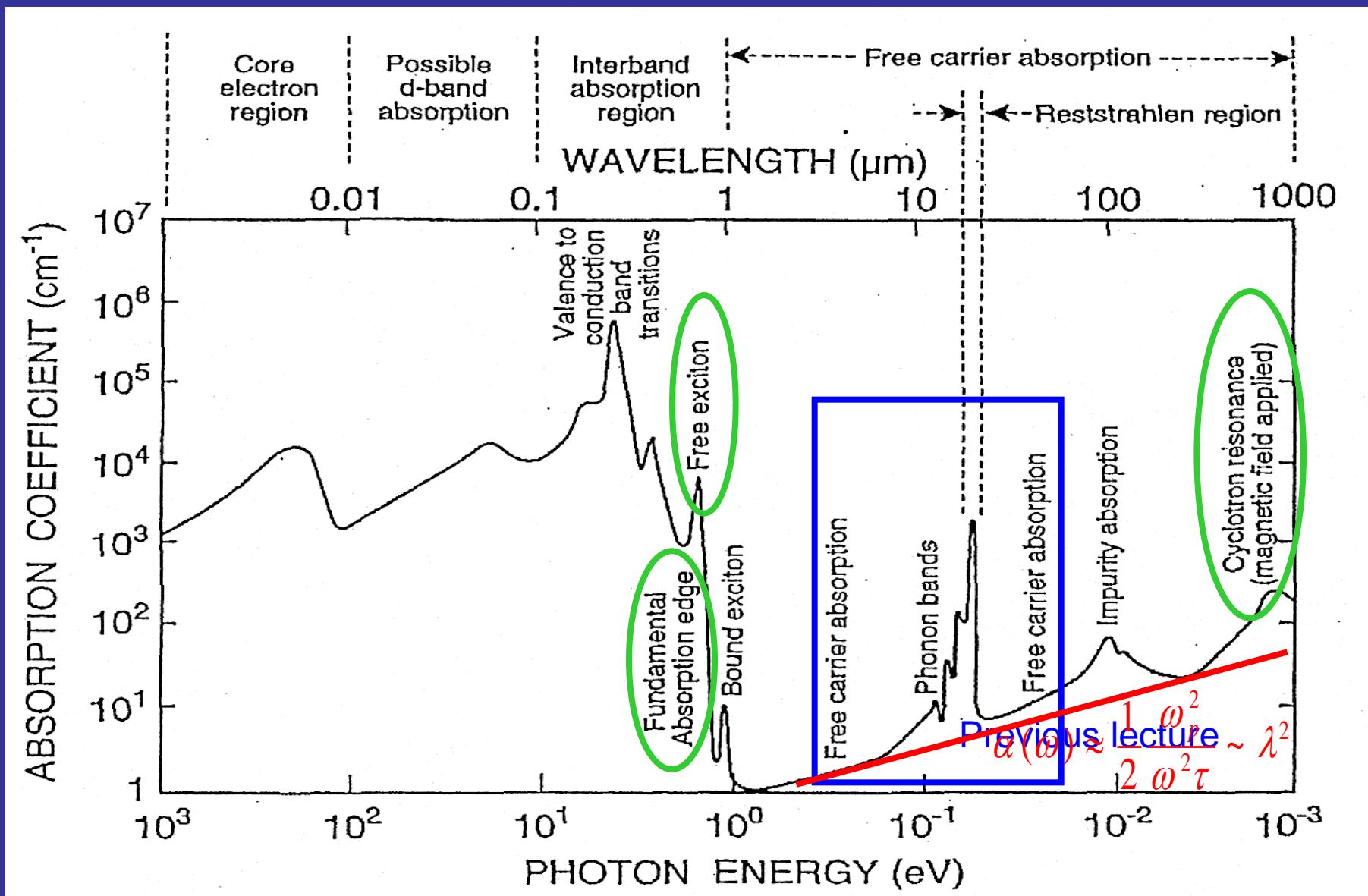
# Overview

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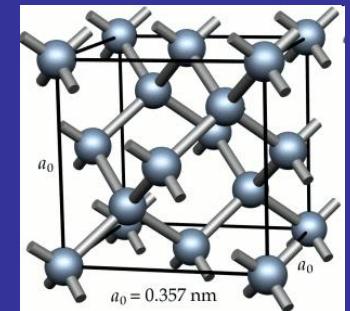
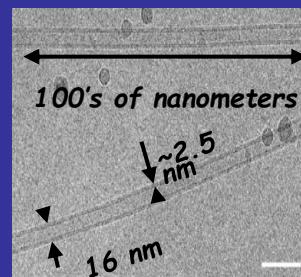
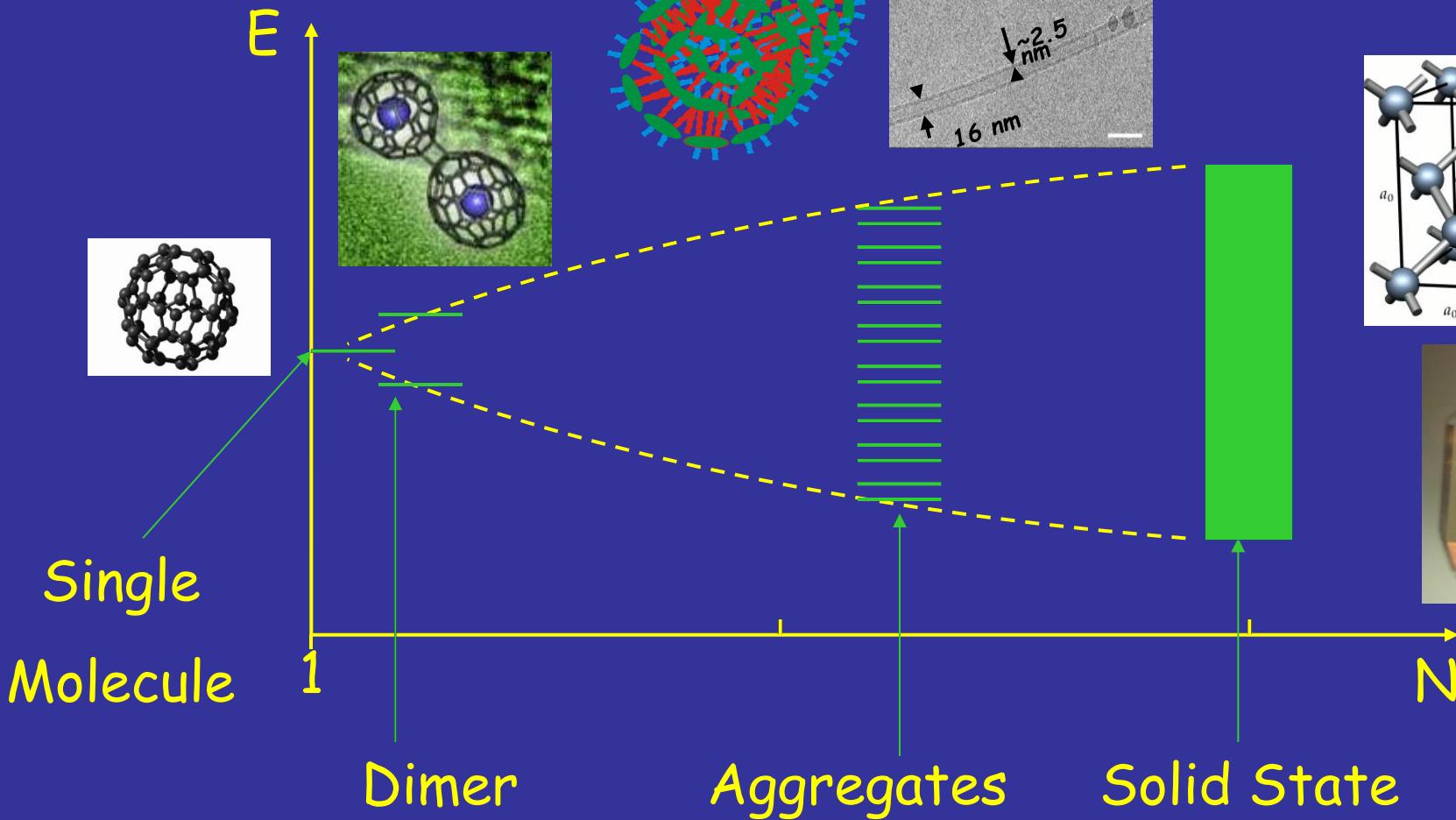
- Introduction (Fox-Ch1)
  - Response function
  - Optical processes
  - Optical constants
- Waves in solids (Fox-Appendix A)
  - Maxwell equations and wave equation
- Models (Fox-Ch2,3,7)
  - Lorentz model
  - Drude-Lorentz model
  - Transition rates, QM treatment
- Magneto-optical effects, XMCD
- Inelastic light scattering
- Non-linear optics
- Time resolved optics
- Optical modification of matter

# Semiconductors (Fox 3)

# Absorption in semiconductors

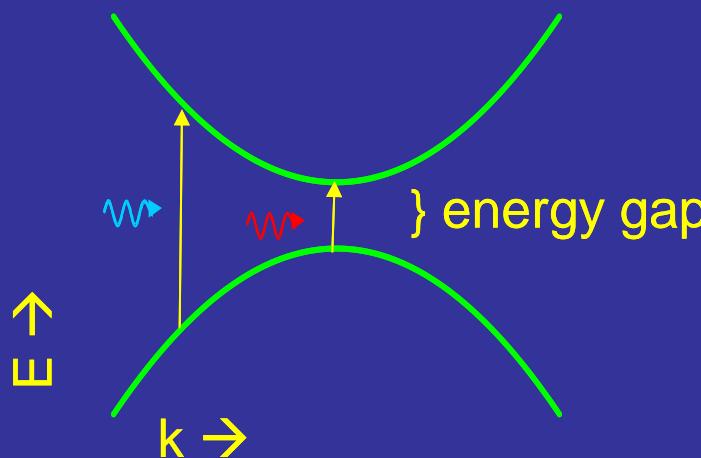


# *Energy bands in solids*



# Fundamental absorption edge

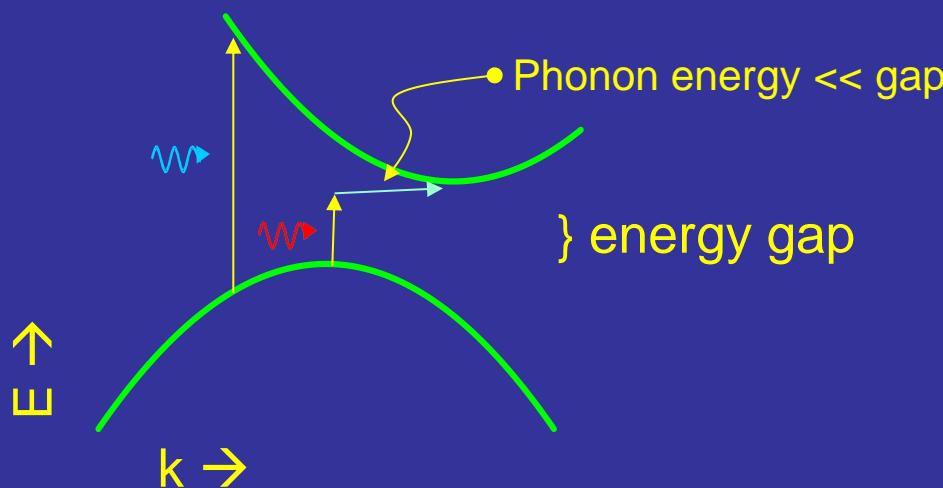
- Direct semiconductors  
‘vertical’ transitions



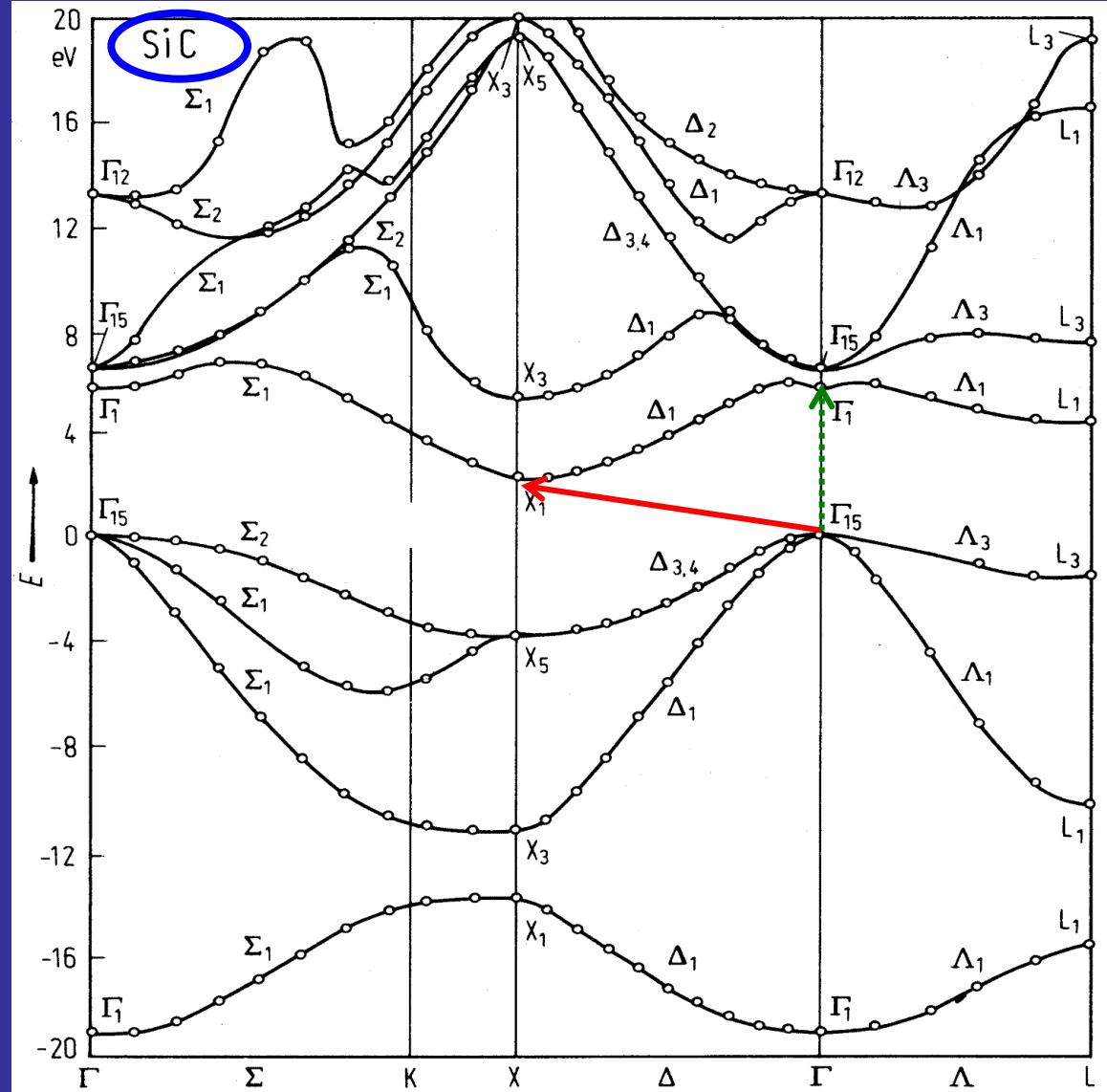
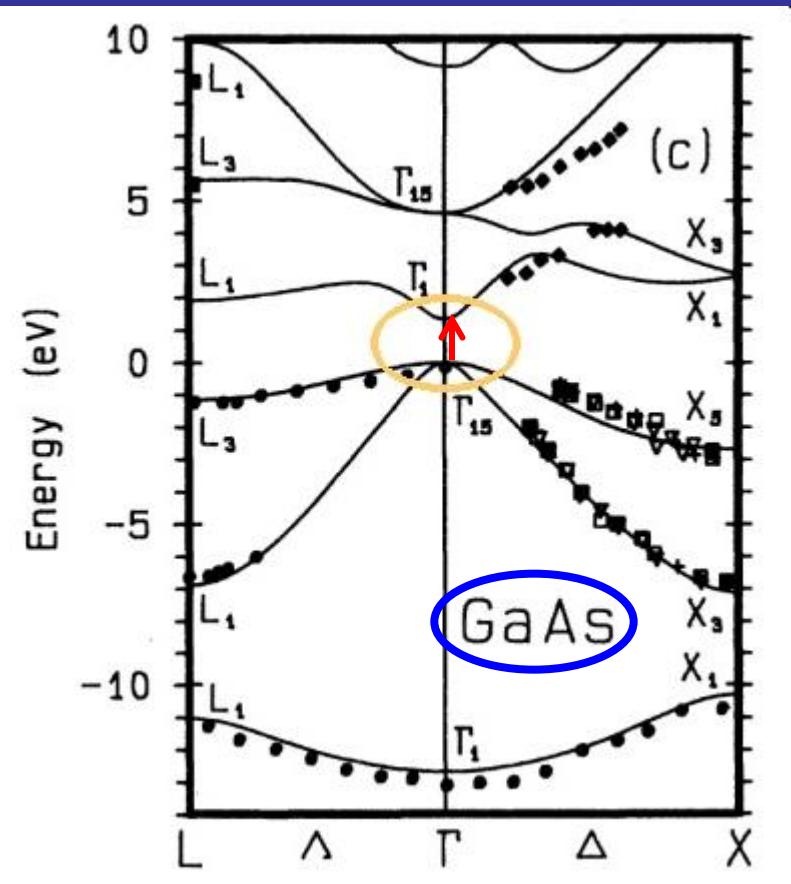
- Indirect semiconductors

Phonon assisted  
(takes up momentum)

Vertical transitions  
for higher  $E$



# GaAs and SiC



# *Transition rates*

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$$\text{Absorption coefficient } \alpha = \frac{\Delta I / I}{\Delta z} = \frac{\text{Rate of E loss/volum e}}{\text{incoming E/area}} = \frac{\hbar\omega \cdot P_{fi} / V}{\hbar\omega / A}$$

Once  $\alpha$  is known, rest of optical functions can be calculated

Task is to calculate the transition rate  $P_{fi} \Rightarrow$  Fermi Golden Rule

# *Optical transitions*

---

- Conservation of energy and momentum

$$E_f = E_i + \hbar\omega$$

$$k_f = k_i + q$$

- Fermi golden rule: transition rate

$$W_{i \rightarrow f} = \frac{2\pi}{\hbar} \left| \langle \phi_f | P | \phi_i \rangle \right|^2 \delta(E_f - E_i - \hbar\omega) \delta(k_f - k_i - q)$$

- Photon momentum  $\sim 0$ , many combinations of states with  $E_f - E_i = \hbar\omega$

$$W_{i \rightarrow f} = \frac{2\pi}{\hbar} |M|^2 g(\hbar\omega)$$

- $g(\hbar\omega)$ : joint density of states

# *Density of states*

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How many states are there in a given interval  $dk$  ? Or in an interval  $dE$  ?

Volume of a sphere in k-space:  $4/3 \pi k^3$

Volume one state occupies in k-space:  $(2\pi/a)^3$

Number of spin degenerate states within the sphere:  $N(k) = 2 \frac{\frac{4}{3} \pi k^3}{\left(\frac{2\pi}{a}\right)^3} = \frac{k^3 a^3}{3\pi^2}$

Density of states:  $D(k) = \frac{1}{V} \frac{dN(k)}{dk} = \frac{k^2}{\pi^2}$

In energy space  $D(E)dE = D(k) \frac{dk}{dE} dE$

For free electrons:

$$D(E) = D(k) \frac{dk}{dE} = \frac{k^2}{\pi^2} \frac{m}{\hbar^2 k} = \frac{m}{\pi^2 \hbar^2} k = \frac{m}{\pi^2 \hbar^2} \frac{\sqrt{2mE}}{\hbar} = \frac{\sqrt{2} m^{3/2}}{\pi^2 \hbar^3} \sqrt{E}$$

# *Bandgap absorption by direct semiconductors*

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- Transition rate proportional to available initial *and* final states

- Initial states: Valence band

$$E_v(k) = -\frac{\hbar^2 k_v^2}{2m_v}$$

- Final states: Conduction band

$$E_c(k) = E_g + \frac{\hbar^2 k_c^2}{2m_c}$$

$$\hbar\omega = E_g + \frac{\hbar^2 k_c^2}{2m_c} + \frac{\hbar^2 k_v^2}{2m_v} = E_g + \frac{\hbar^2 k^2}{2\mu} \text{ using } k = k_v = k_c \text{ and } \frac{1}{\mu} = \frac{1}{m_v} + \frac{1}{m_c}$$

- JDOS: For  $\hbar\omega < E_g$  :  $g(\hbar\omega) = 0$

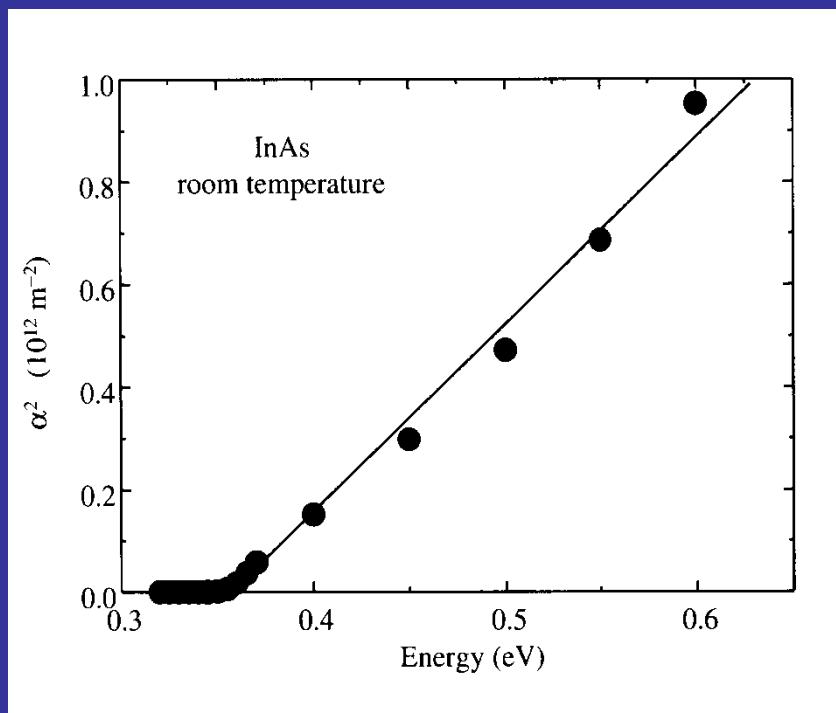
$$\text{For } \hbar\omega > E_g : g(\hbar\omega) = \frac{\sqrt{2}\mu^{3/2}}{\pi^2\hbar^3} \sqrt{\hbar\omega - E_g}$$

# Direct transitions

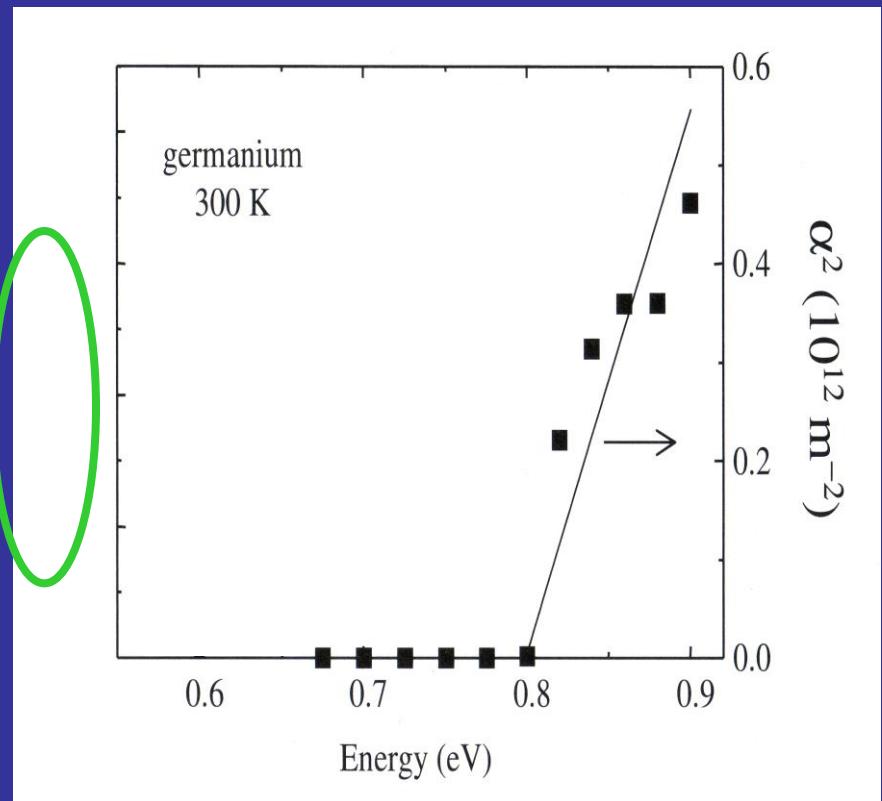
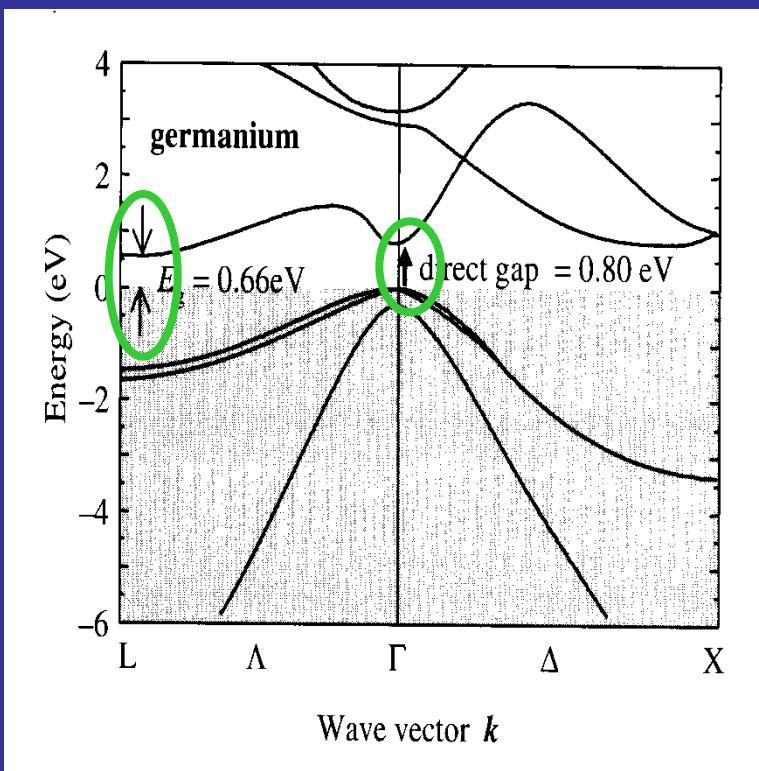
- Absorption coefficient proportional to transition rate  $\alpha = -\frac{1}{I} \frac{dI}{dz} \propto W_{i \rightarrow f}$   
(beer's law:  $dI = -\alpha z I(z) \rightarrow I(z) = I_0 e^{-\alpha z}$ )

For  $\hbar\omega < E_g$  :  $\alpha(\hbar\omega) = 0$

For  $\hbar\omega > E_g$  :  $\alpha(\hbar\omega) \propto \mu^{3/2} \sqrt{\hbar\omega - E_g}$



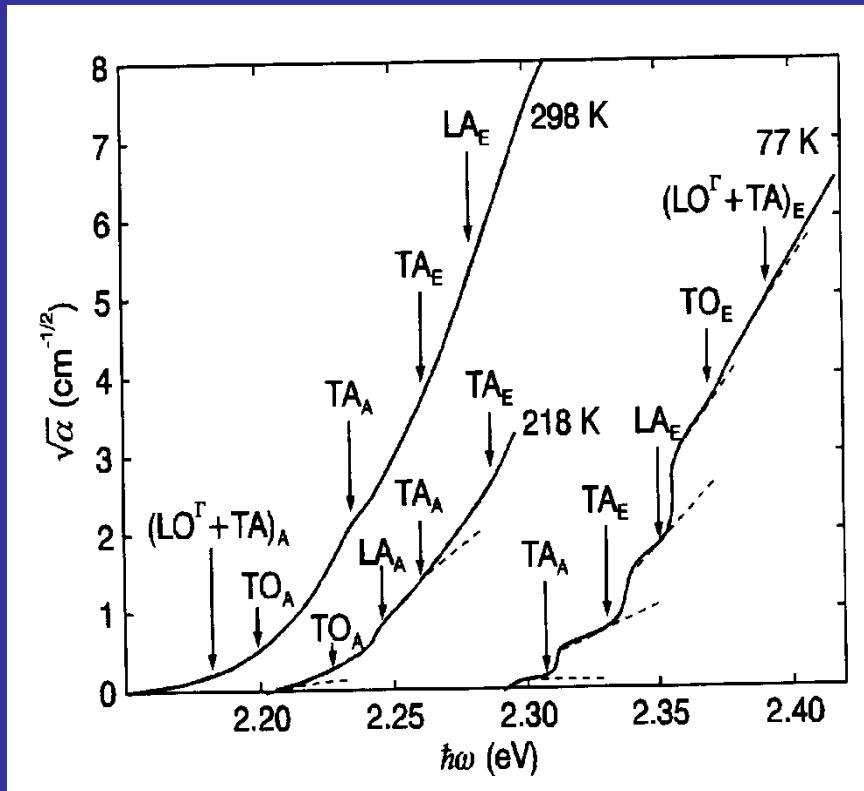
# Germanium



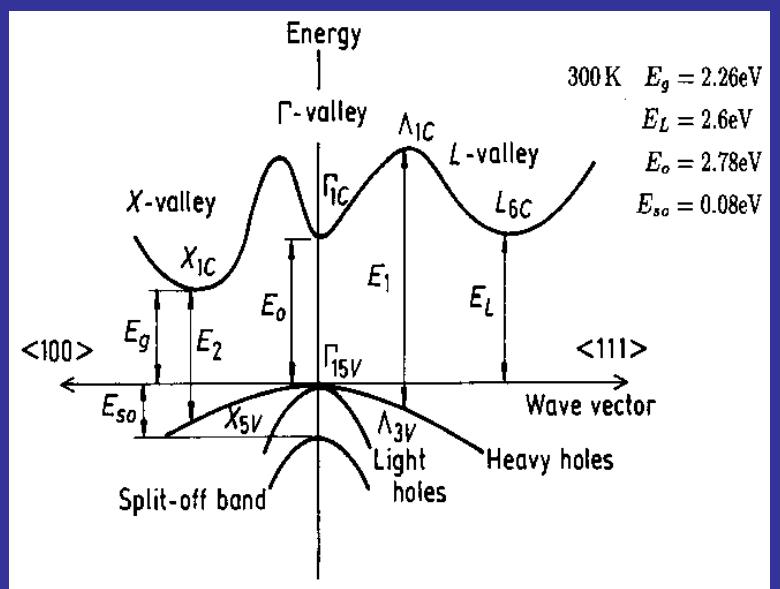
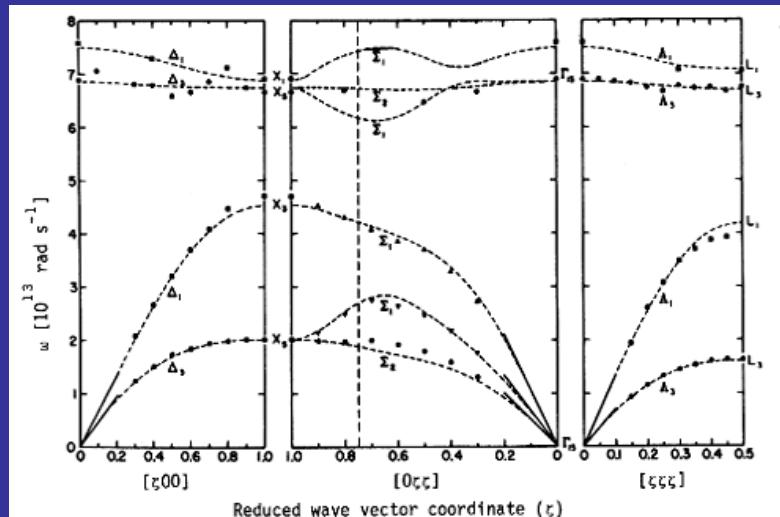
$$\text{Direct gap : } \alpha(\hbar\omega) \propto \sqrt{\hbar\omega - E_g}$$

$$\text{Indirect gap (not derived here) : } \alpha(\hbar\omega) \propto (\hbar\omega - E_g \mp \hbar\Omega)^2$$

# GaP phonon structure



$$\text{Indirect gap : } \alpha(\hbar\omega) \propto (\hbar\omega - E_g \mp \hbar\Omega)^2$$



# Semiconductors *in a magnetic field*

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- At high enough fields: quantization of orbits and energy

$$E_n = \left( n + \frac{1}{2} \right) \hbar \omega_c$$

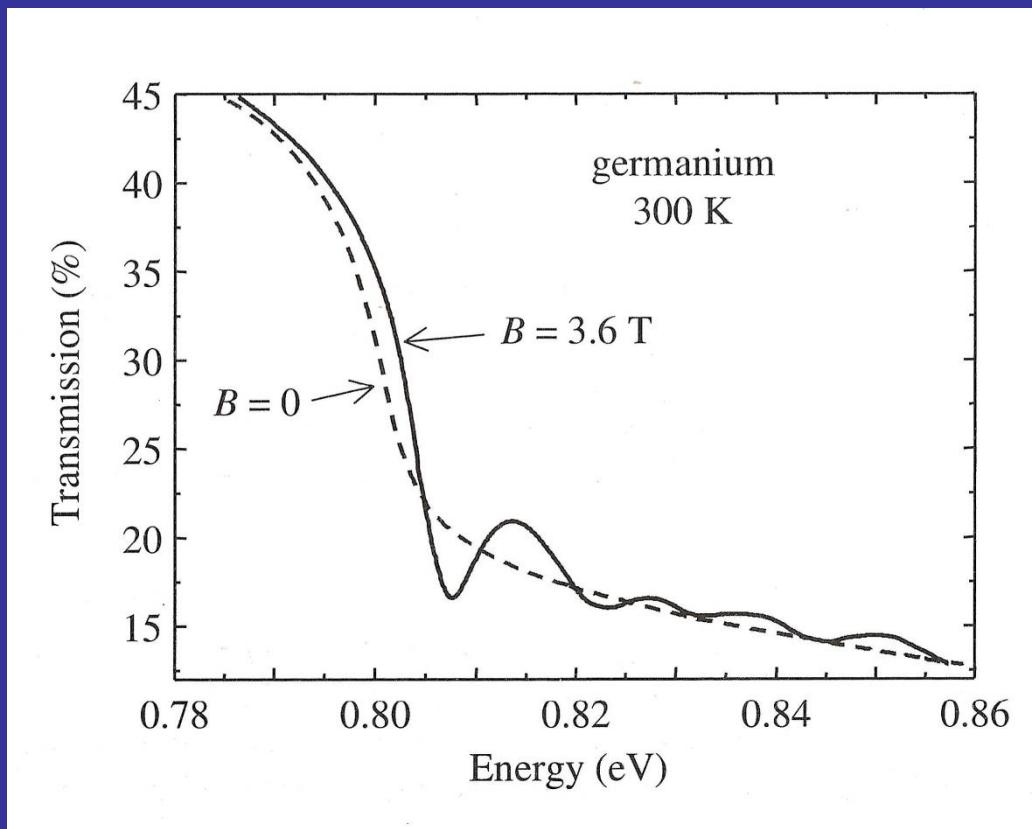
- For  $B=B_z$ :  $E_n^v(k_z) = -\left( n + \frac{1}{2} \right) \hbar \frac{eB}{m_h^*} - \frac{\hbar^2 k_z^v{}^2}{2m_h^*}$

$$E_n^c(k_z) = E_g + \left( n + \frac{1}{2} \right) \hbar \frac{eB}{m_e^*} + \frac{\hbar^2 k_z^c{}^2}{2m_e^*}$$

$$\hbar \omega = E_g + \left( n + \frac{1}{2} \right) \hbar \frac{eB}{\mu} + \frac{\hbar^2 k_z^2}{2\mu}$$

- Strong absorption for  $k_z=0$   
→ equidistant peaks in absorption spectrum  $\hbar \omega = E_g + \left( n + \frac{1}{2} \right) \hbar \frac{eB}{\mu}$
- Absorption edge shift in magnetic field  $\Delta = \hbar \frac{eB}{2\mu}$

# *Ge in a magnetic field*



PHYSICAL REVIEW

VOLUME 108, NUMBER 6

DECEMBER 15, 1957

## Oscillatory Magneto-Absorption in Semiconductors\*

SOLOMON ZWERDLING, BENJAMIN LAX, AND LAURA M. ROTH

*Lincoln Laboratory, Massachusetts Institute of Technology, Lexington, Massachusetts*

(Received August 30, 1957)

# Cyclotron resonance

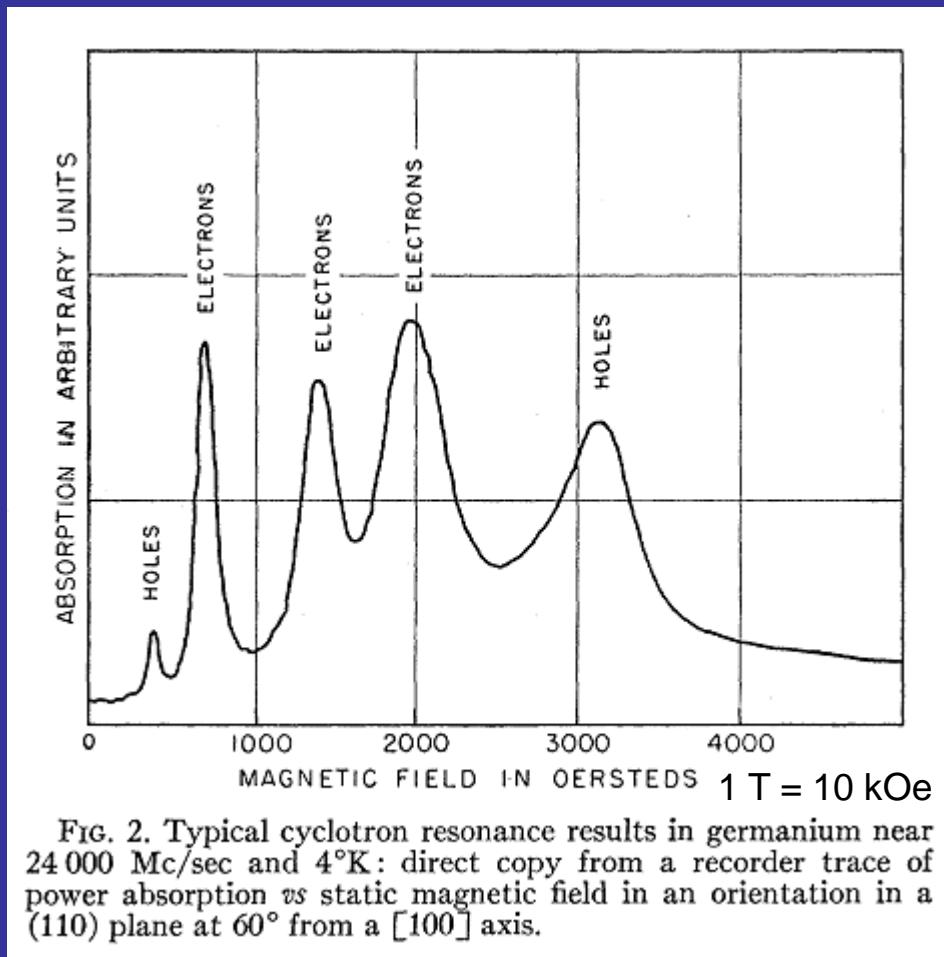


FIG. 2. Typical cyclotron resonance results in germanium near 24 000 Mc/sec and 4°K: direct copy from a recorder trace of power absorption vs static magnetic field in an orientation in a (110) plane at 60° from a [100] axis.

- Transitions with  $\Delta n = 1$
- 24000 Mc/sec  $\sim 1$  meV
- Energy fixed, scan B

$$\omega_c = \frac{eB}{m^*} \Rightarrow \text{determine effective mass}$$

## Cyclotron Resonance of Electrons and Holes in Silicon and Germanium Crystals

G. DRESSELHAUS, A. F. KIP, AND C. KITTEL  
Department of Physics, University of California, Berkeley, California  
(Received December 16, 1954)

# *Wannier-Mott Excitons*

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- Conduction band: electrons with mass  $m_e^*$
- Valence band: holes with mass  $m_h^*$
- Hydrogen problem with very light ‘proton’ in a screened environment

- Screening:  $e^2 \rightarrow e^2 / \epsilon_r$

- Reduced mass:  $m_e \rightarrow \mu = \left[ \frac{1}{m_e} + \frac{1}{m_h} \right]^{-1}$

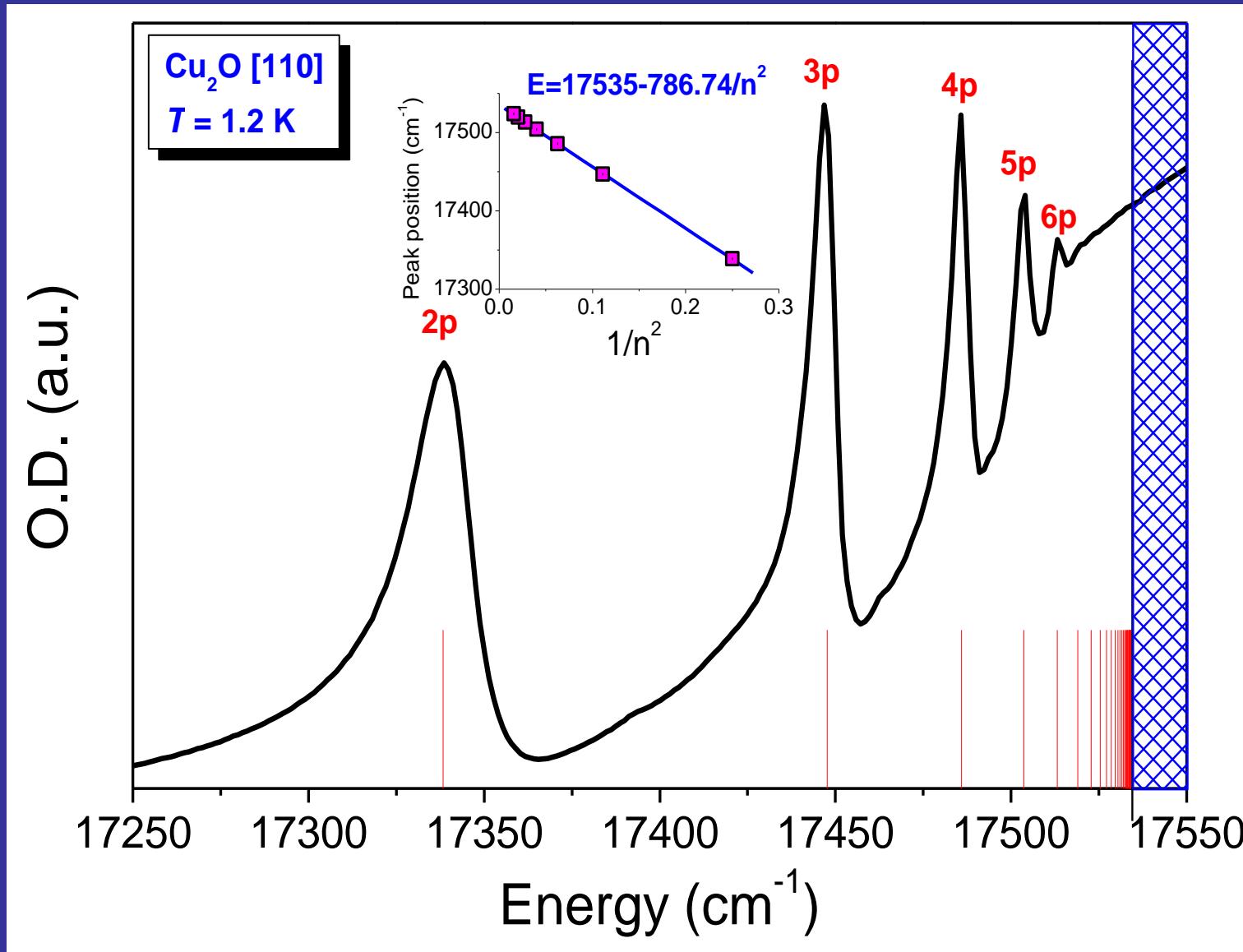
$$H = \frac{p_e^2}{2m_e} + \frac{p_p^2}{2m_p} - \frac{e^2}{|r_e - r_p|} \Rightarrow H = \frac{p_e^2}{2m_e^*} + \frac{p_h^2}{2m_h^*} - \frac{e^2}{\epsilon_r |r_e - r_h|}$$

$$a_{ex} / a_H = \frac{m_e}{\mu} \epsilon_r \approx 20$$

$$E_{ex} / E_H = \frac{\mu}{m_e} \frac{1}{\epsilon_r^2} \approx \frac{1}{144}$$

	Hydrogen	Cu <sub>2</sub> O
Bohr radius	0.53 Å	10.6 Å
Binding E <sub>1</sub>	13.6 eV	94 meV

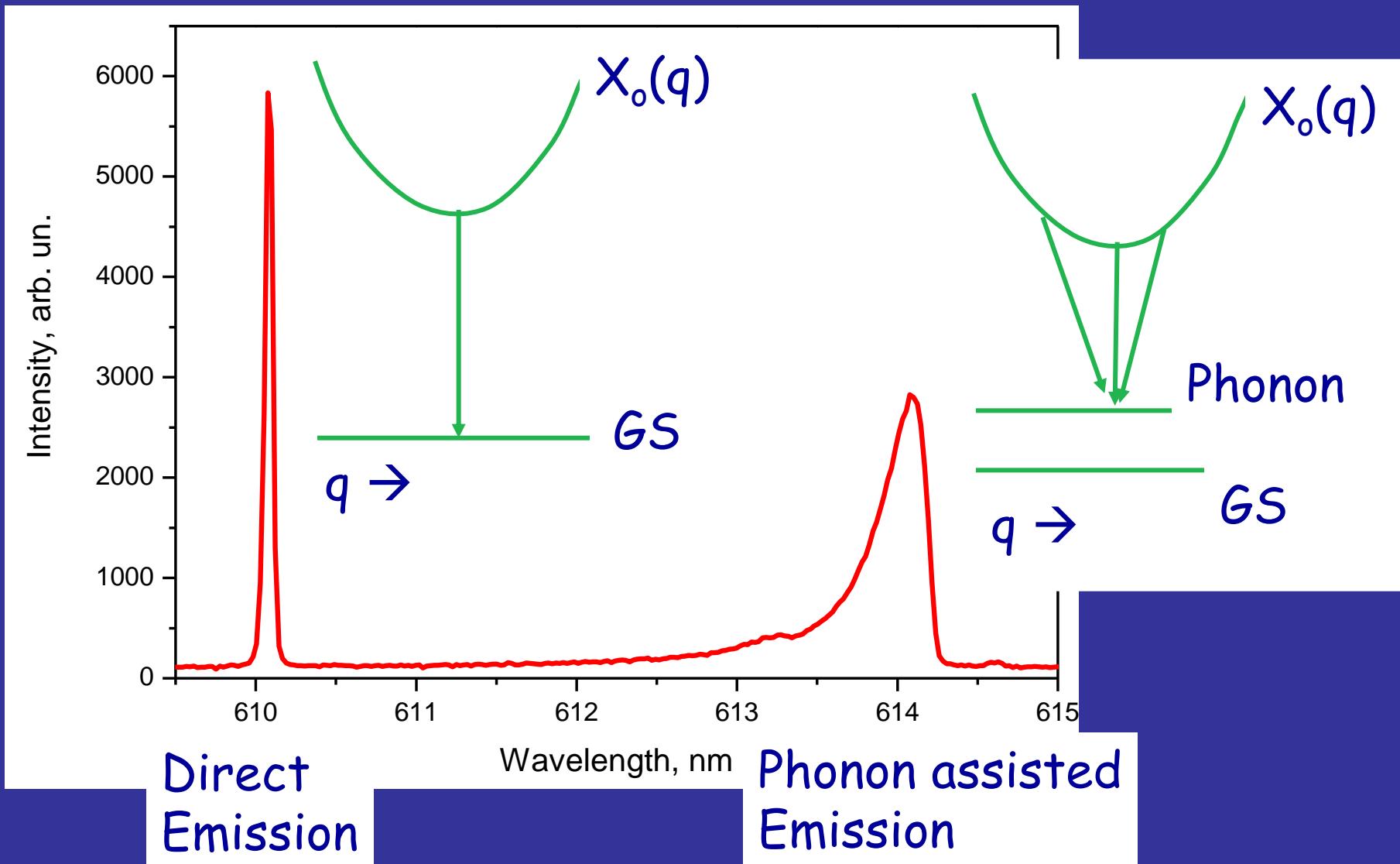
# Excitons in $Cu_2O$ (absorption)



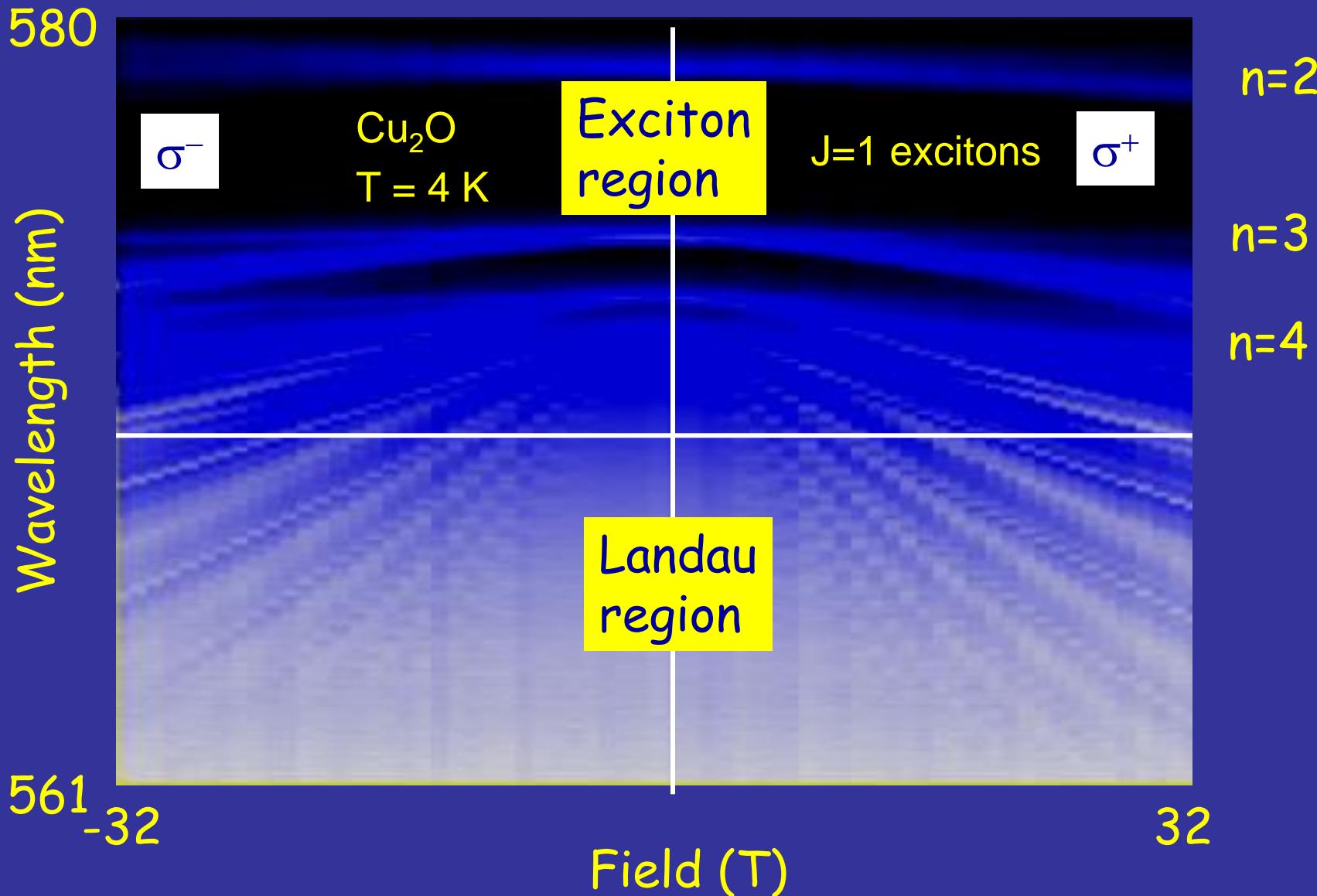
Lyman series

$$E(n) = \frac{E_0}{n^2}$$

# $Cu_2O$ Emission



# Magneto-absorption of excitons



# Excitons in KBr

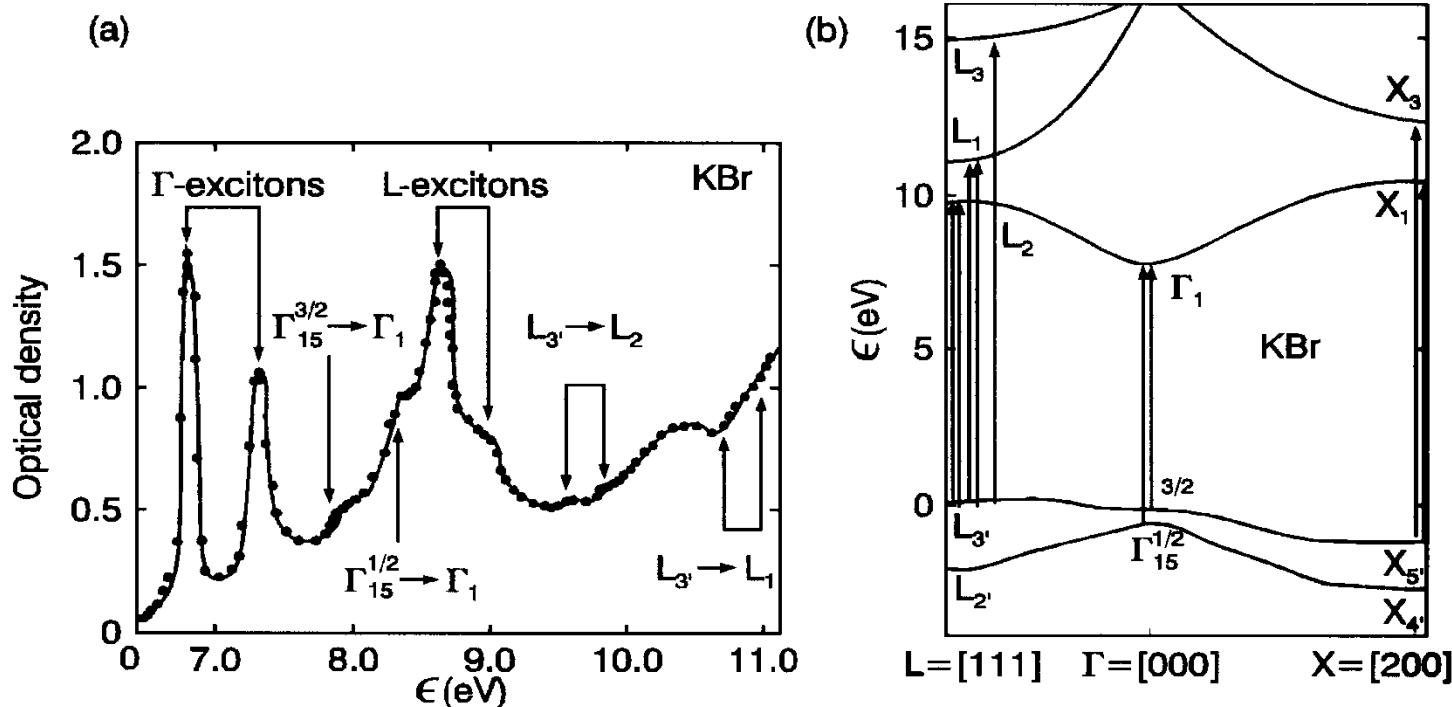


Fig. 7.7. Optical density for KBr measured at 80 K (a) and band structure for the corresponding lattice (b); after [7.11].

PHYSICAL REVIEW

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## Ultraviolet Absorption of Alkali Halides\*

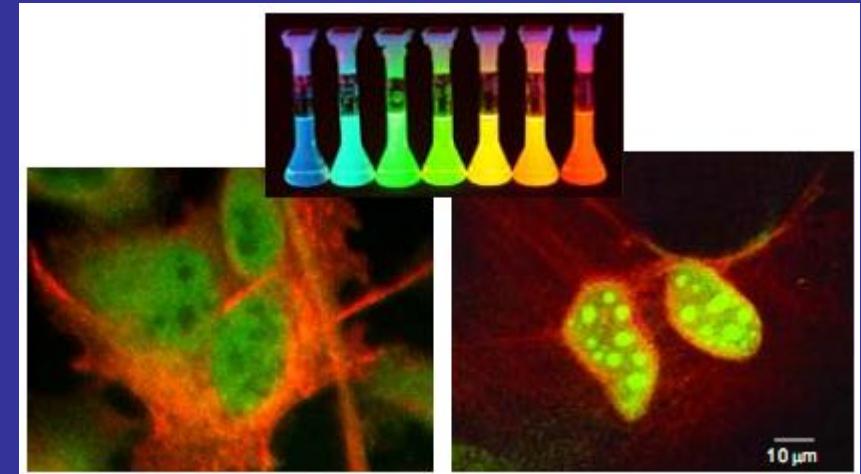
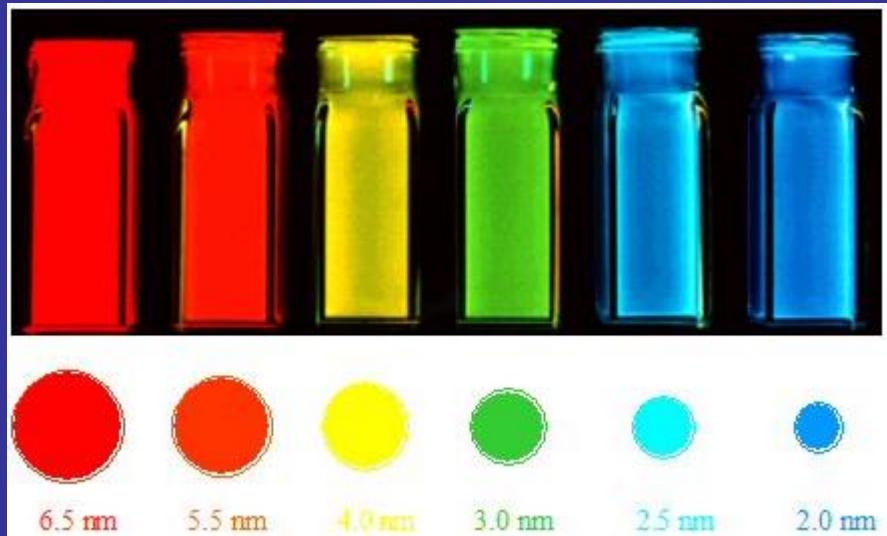
J. E. EBY,<sup>†</sup> K. J. TEEGARDEN, AND D. B. DUTTON

Institute of Optics, University of Rochester, Rochester, New York

(Received May 27, 1959; revised manuscript received August 19, 1959)

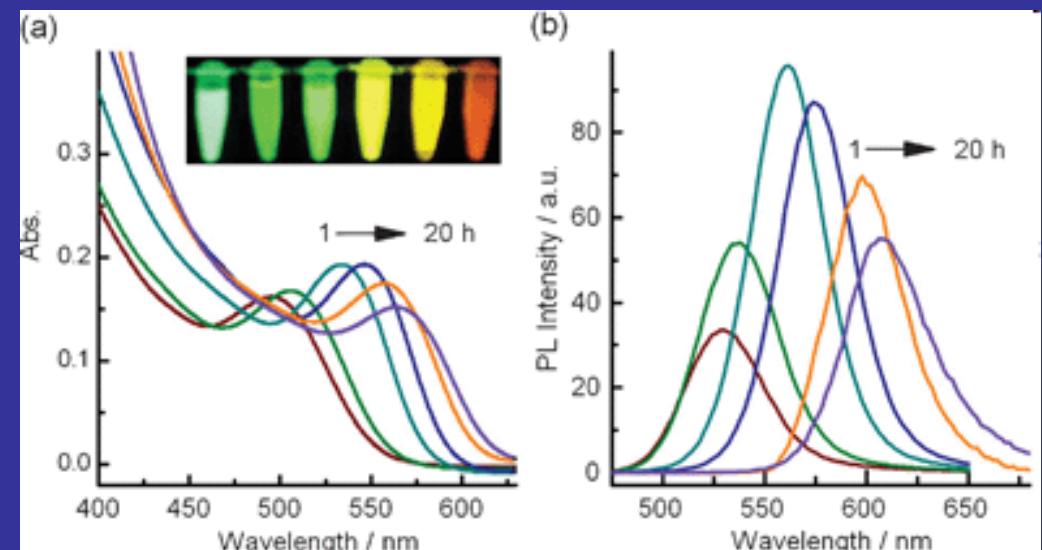
# Nano Crystals

## CdSe nanocrystals



## CdTe nanocrystals

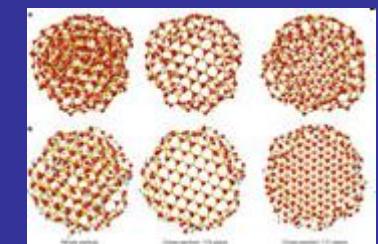
- Bio labeling
- Displays
- Solar cells
- Photonic crystals
- MRI enhancement
- ...



# Nano Crystals

Bandgap CdTe: 1.56 eV (direct)

Bulk → emission at 795 nm



Small particle: confinement energy (particle in a box)

$$E = E_g + \frac{\hbar^2 \pi^2}{2 \mu R^2}$$

$$\left. \begin{array}{l} \text{CdTe: } m_e^* \approx 0.1 m_0 \\ m_h^* \approx 0.44 m_0 \end{array} \right\} \mu \approx 0.08 m_0$$

2 nm particles: Confinement 1.15 eV

$E = 1.56 + 1.15 = 2.71$  eV Corresponds to 475 nm

For 3 nm: 600 nm

