Magnetism

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Lectures

Last time	Introduction	Ch.1; 2.1-2.5; 8.9
Today	**Moments, interactions, environment**	**3.1, Ch.4; 7.1-7.7**

Magnetism

Origin of magnetism

- Orbital magnetism (p → p+eA)
- Spin magnetism (spin S, localized, itinerant)

Magnetic interactions

- Dipole
- Exchange interaction (direct, indirect)
- RKKY (itinerant exchange)
- Double exchange
- Anisotropic exchange (LS interaction)

Magnetism

Diamagnetism:

- No magnetic moments
- No magnetic interaction
- Response due to induced currents
- Magnetization opposite to field

Paramagnetism:

- Magnetic moments (spin, orbit)
- Weak magnetic interactions
- Response due to orientation
- Magnetization in field direction

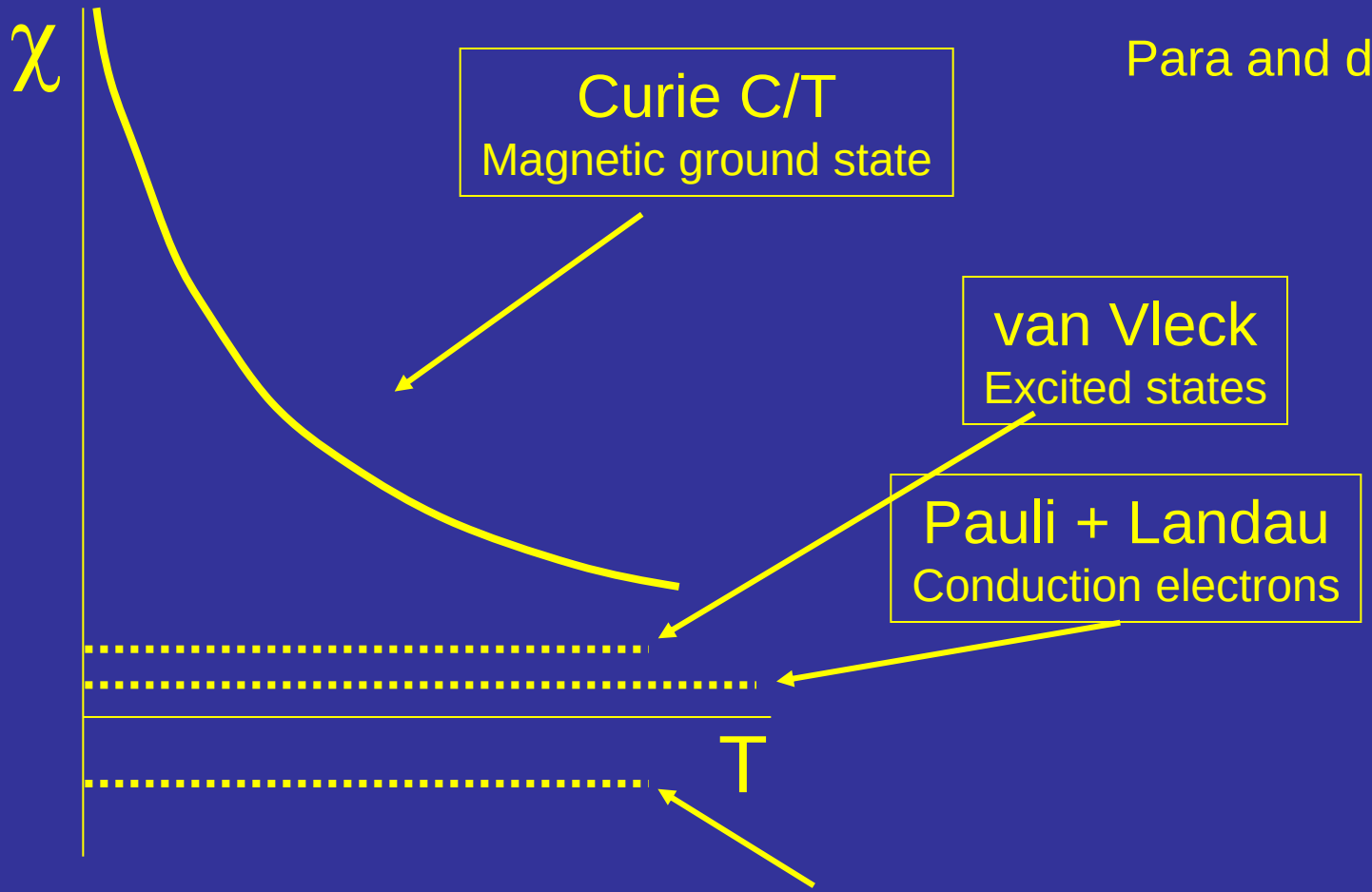
Ordered magnetism:

- Magnetic moments
- Strong magnetic interactions
- Response due to polarization
- Ferro-, antiferro-, ferrimagnetic

‘Non-ordering magnetism’

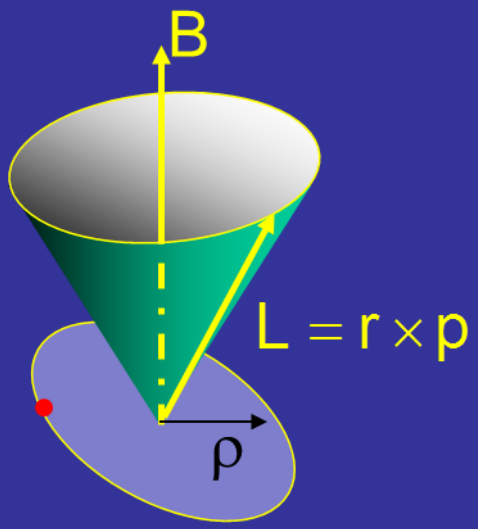
Magnetism

Para and diamagnetism



$$M = \chi H$$

‘Classical’ Langevin diamagnetism



e^- in B-field => Larmor precession with $\omega_L = \frac{eB}{2mc}$

Current of Z electrons per atom $I = -Ze \cdot \frac{\omega_L}{2\pi}$

Magnetic moment

$$\mu = I \cdot A = I \cdot \pi \langle \rho^2 \rangle = -\frac{Ze^2 B}{4mc^2} \cdot \langle \rho^2 \rangle$$

Susceptibility of n atoms/volume

$$\chi = \frac{n\mu}{B} = -\frac{nZe^2}{6mc^2} \cdot \langle r^2 \rangle$$

Force: $F = M \frac{\partial H}{\partial x}$

Floating matter (magnetic levitation)

(perfect) diamagnetism

Floating $YBaCuO_{6+d}$

1986: J.G. Bednorz
& K.A. Mueller

Magnetic moments

- Intrinsic magnetic moment of elementary particles: Spin
- Moving charges: Orbits

- Spin-orbit coupling ➔ J; m_J
- Magnetic moment:

$$\mu = g_J \sqrt{J \cdot (J+1)}\,\mu_B$$

$$\mu_z = g_J \cdot m_J \cdot \mu_B$$

- Energy in a field

$$E = g_J \cdot m_J \cdot \mu_B \cdot B$$

- Free electron spin (S=1/2) in 1 T:

$$\mu_s \approx 1.73\,\mu_B \qquad E \approx 60\,\mu\text{eV} \therefore 0.7\ \text{K}$$

Only orbits: $g_l=1$
Only electron spin: $g_s=2$
More general:

$$g_J = \frac{3J(J+1) + S(S+1) - L(L+1)}{2J(J+1)}$$

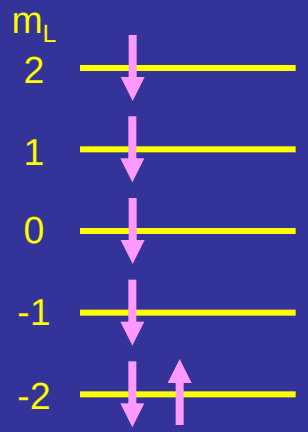
Bohr magneton

$$\mu_B = \frac{\hbar e}{2m_e} = 9.274\ \text{J/T}$$
$$= 5.7553 \cdot 10^{-5}\ \text{eV/T}$$

Localized moments: partially filled shells

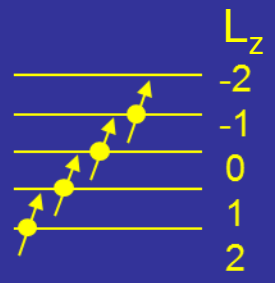
- d-levels, f-levels
- L-S coupling scheme
- Hund's rules
  1. **Maximize S** (→ spatially antisymmetric, decrease shielding)
  2. **Maximize L** (→ orbiting in same direction, decrease repulsion)
  3. **J=|L-S| for < half full**
     J=|L+S| for > half full (→minimize LS interaction)

example Fe^{2+}: [Ar]$3d^6$
6 electrons
Total spin: 2
Total L: 2
➔J=4
Term symbol ($^{(2s+1)}L_J$): $^5D_4$



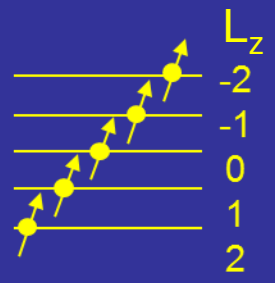
Some more examples

d-shell (L = 2), 4 electrons
Mn^{3+},Cr^{2+}



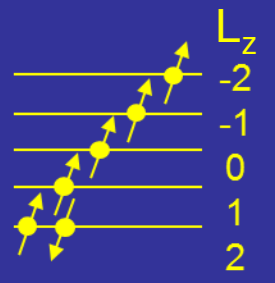
S=2
L=2 => $^5D_0$
J=0

d-shell (L = 2), 5 electrons
Fe^{3+},Mn^{2+}



S=5/2
L=0 => $^6S_{5/2}$
J=5/2

d-shell (L = 2), 6 electrons
Fe^{2+}



S=2
L=2 => $^5D_4$
J=4

Environment: crystal field

Rare earth's: 4f shell's small ('inner' electrons)
Iron group: 3d shell's on the outside

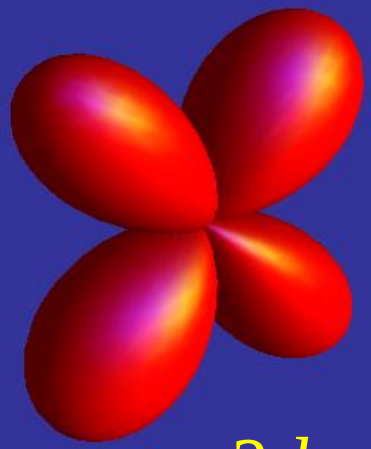
=> decoupling of L and S, J no longer good Quantum number
=> splitting of the 2L+1 orbital states
=> Quenching of the orbital angular momentum ($L_z \rightarrow 0$)

=> High spin – Low spin transitions
=> Jahn-Teller distortions
=> Orbital excitations (orbitons)

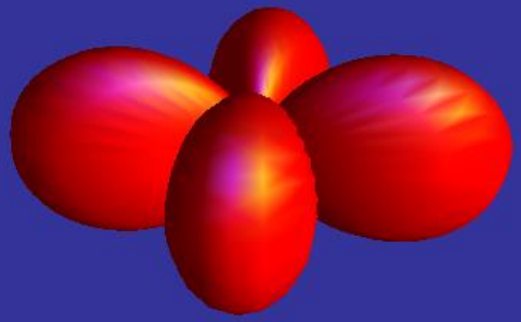
Anisotropy

Kramers degeneracy (local B-field probe)

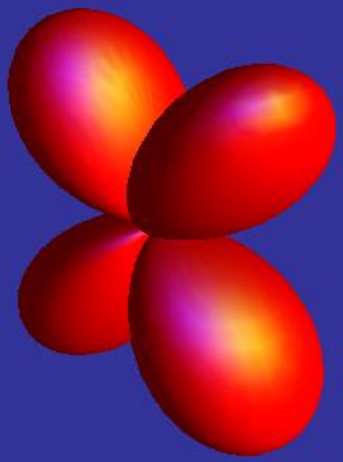
3d orbitals (Chem)



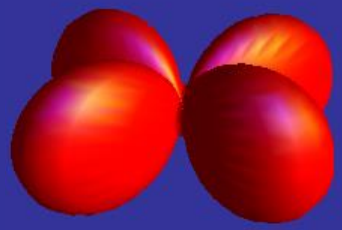
$3d_{xz}$



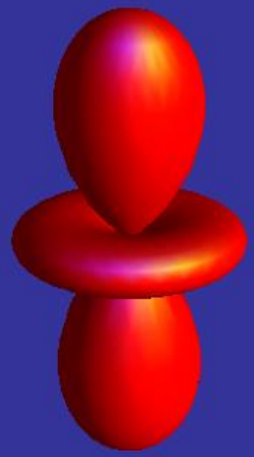
$3d_{xy}$



$3d_{yz}$

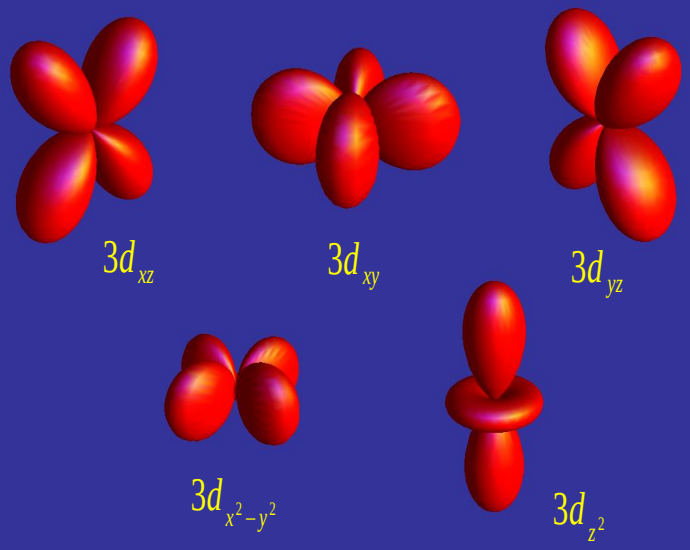


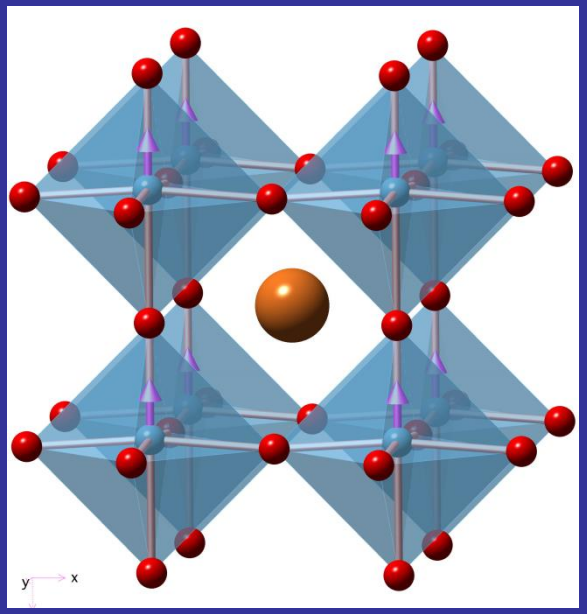
$3d_{x^2-y^2}$



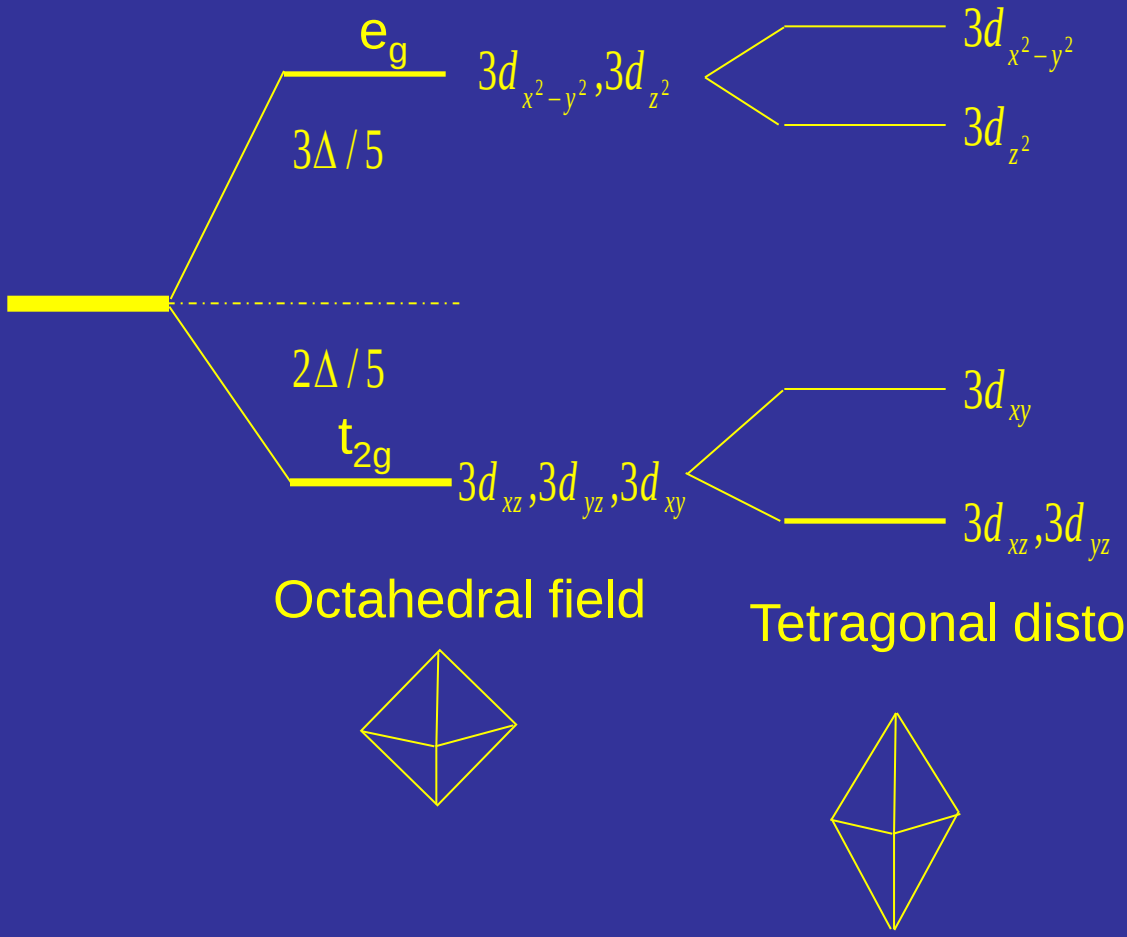
$3d_{z^2}$

3d orbitals in a CF

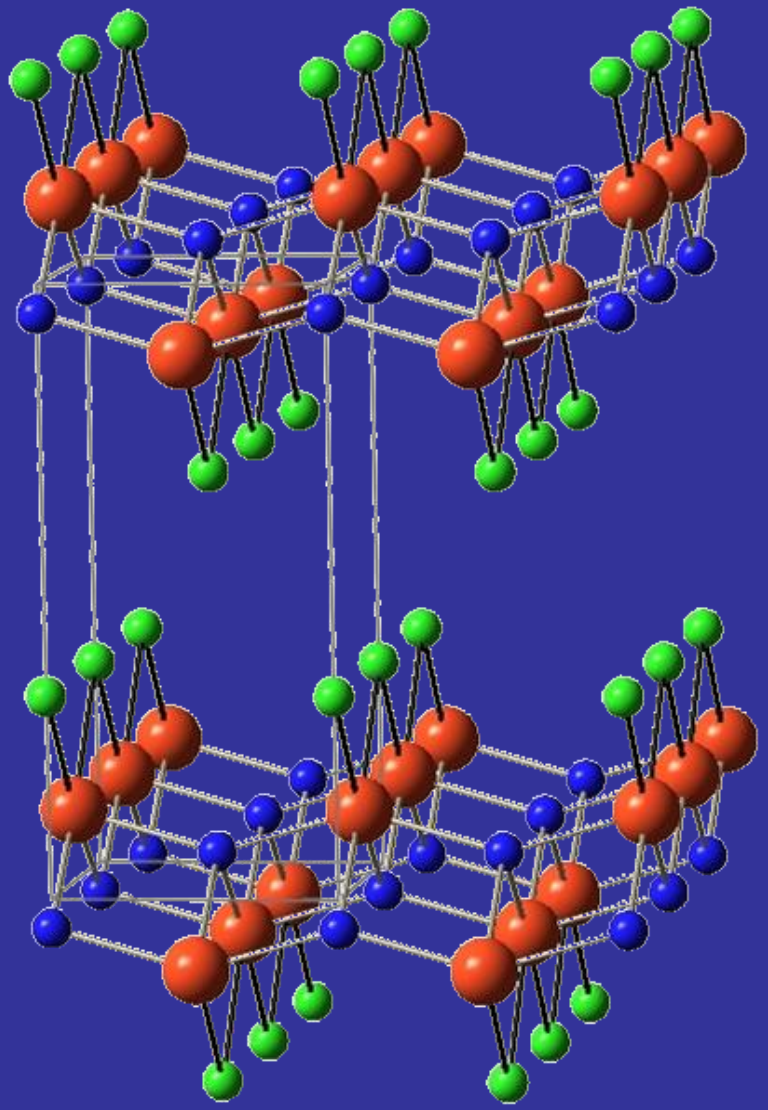




Perovskite structure (ABO_3 e.g. $BaTiO_3$)



TiOX



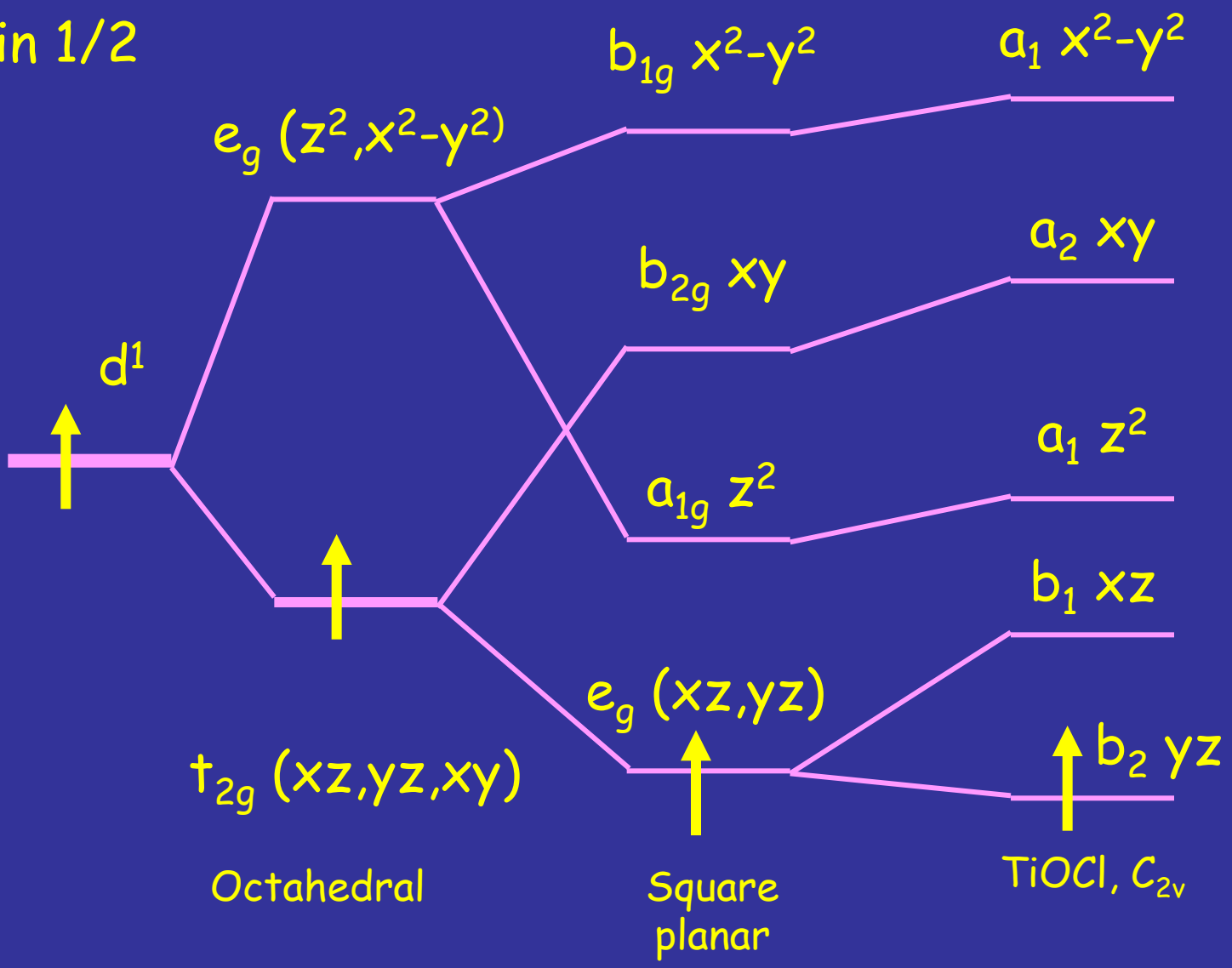
Pmmn

Double bi-layer of
TiO_4Cl_2 "Octaedra"

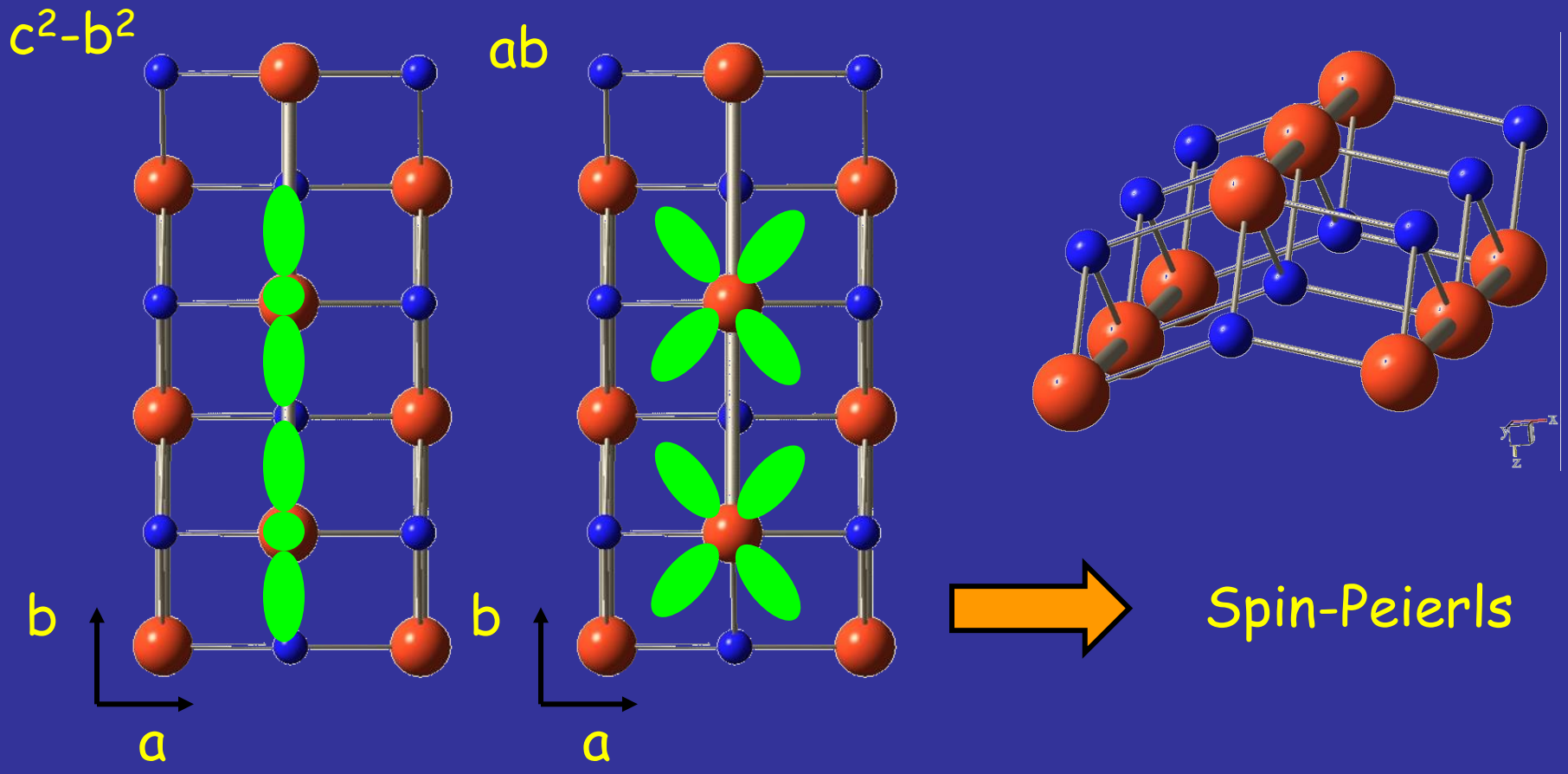
Layered:
Cl-Cl distance 3.7 Å

3d levels in TiOX

Ti^{+} $3d^1$, spin 1/2

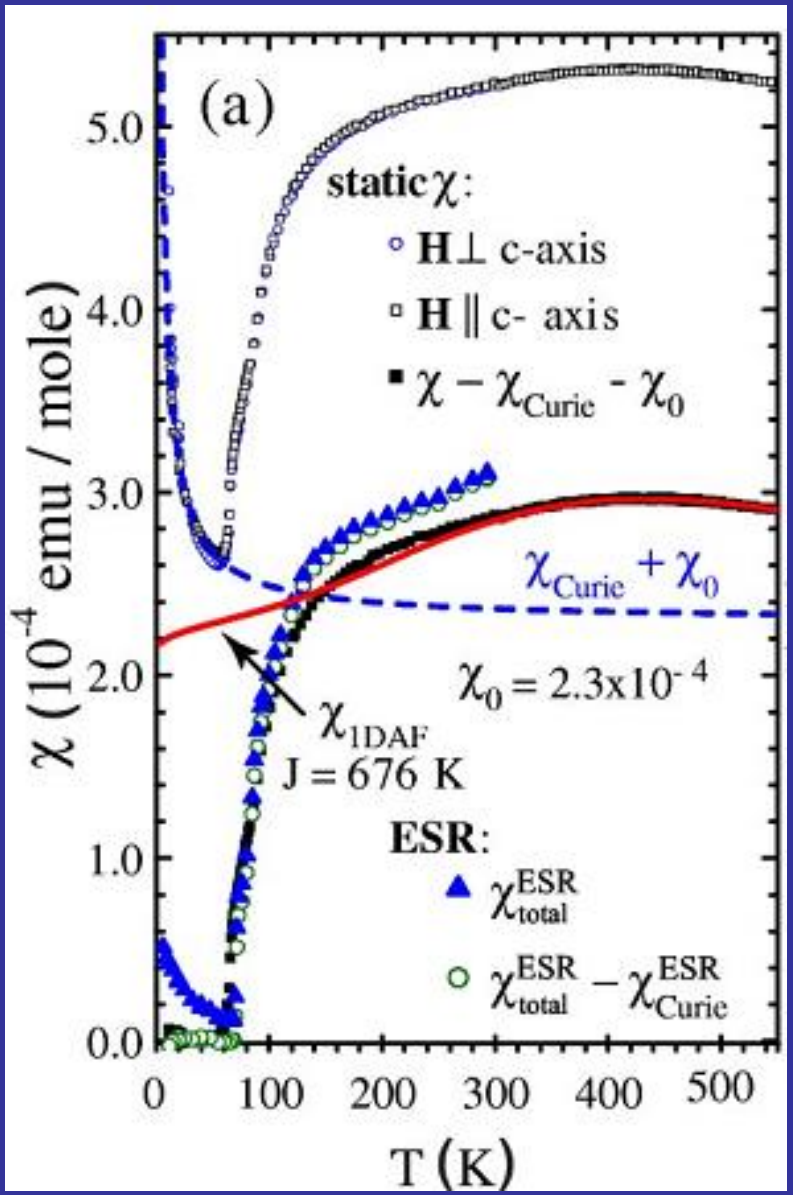


Occupied orbitals



Exchange through direct Ti-Ti interaction along b ➔ 1D system
Mott-Hubbard ➔ AF interaction

Susceptibility TiOX



Kataev et al., PRB 68, 140405 (2003)

Above T_c: Typical 1D Heisenberg AF
Below T_c: Opening of a gap due to dimerization