

Last time

- Raman effect (Fox 10.5)
- Metals (Fox 7)
- Semiconductors (Fox 3)

- Remainder semiconductors (Fox 3)

Semiconductors in a magnetic field

- At high enough fields: quantization of orbits and energy

$$E_n = \left(n + \frac{1}{2} \right) \hbar \omega_c$$

- For $B=B_z$: $E_n^v(k_z) = -\left(n + \frac{1}{2} \right) \hbar \frac{eB}{m_h^*} - \frac{\hbar^2 k_z^v}{2m_h^*}$

$$E_n^c(k_z) = E_g + \left(n + \frac{1}{2} \right) \hbar \frac{eB}{m_e^*} + \frac{\hbar^2 k_z^c}{2m_e^*}$$

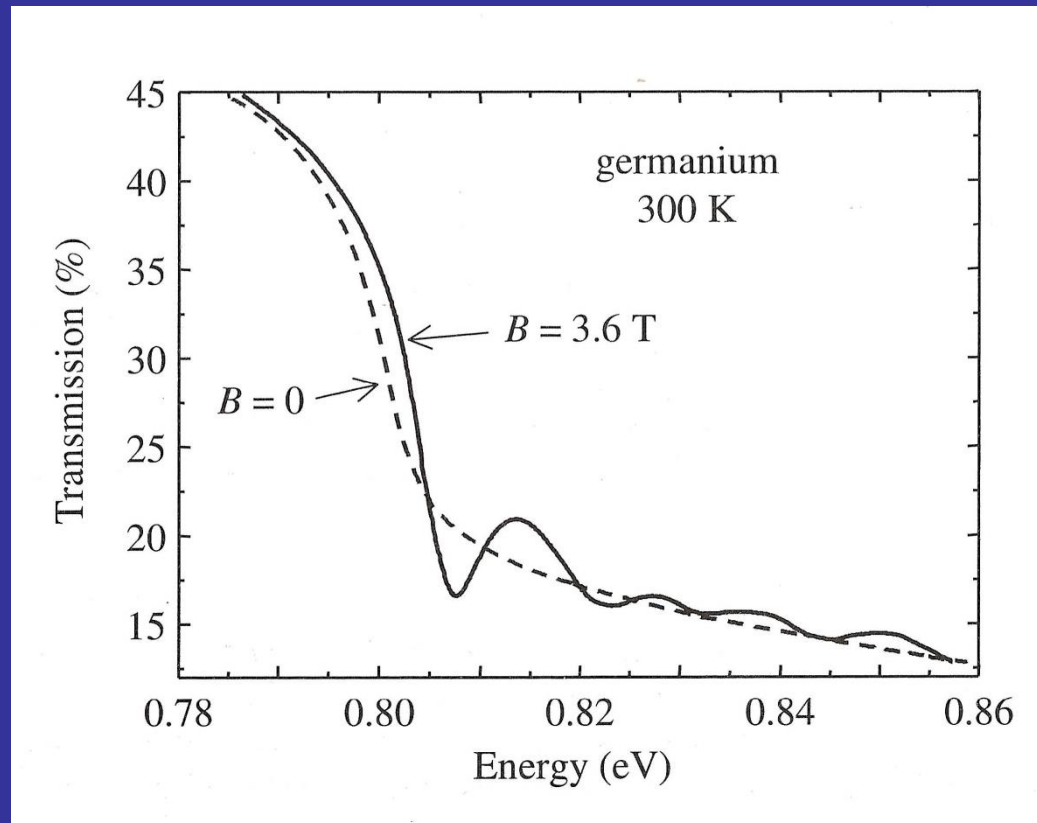
$$\hbar \omega = E_g + \left(n + \frac{1}{2} \right) \hbar \frac{eB}{\mu} + \frac{\hbar^2 k_z^2}{2\mu}$$

- Strong absorption for $k_z=0$

→ equidistant peaks in absorption spectrum $\hbar \omega = E_g + \left(n + \frac{1}{2} \right) \hbar \frac{eB}{\mu}$

- Absorption edge shift in magnetic field $\Delta = \hbar \frac{eB}{2\mu}$

Ge in a magnetic field



PHYSICAL REVIEW

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Oscillatory Magneto-Absorption in Semiconductors*

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(Received August 30, 1957)

Cyclotron resonance

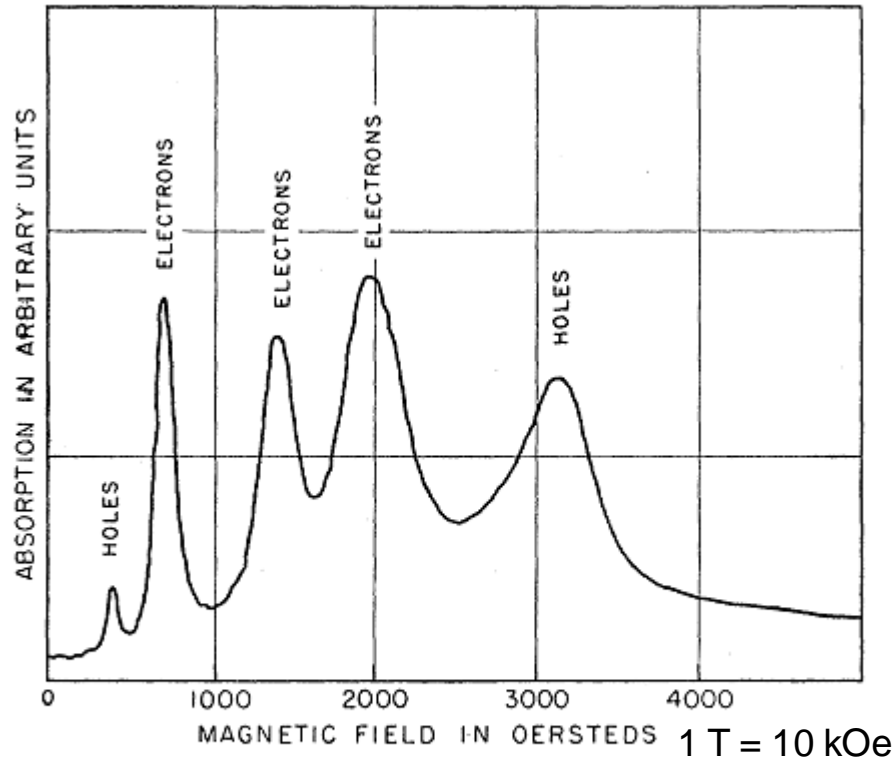


FIG. 2. Typical cyclotron resonance results in germanium near 24 000 Mc/sec and 4°K: direct copy from a recorder trace of power absorption vs static magnetic field in an orientation in a (110) plane at 60° from a [100] axis.

- Transitions with $\Delta n = 1$
- 24000 Mc/sec \sim 1 meV
- Energy fixed, scan B

$$\omega_c = \frac{eB}{m^*} \Rightarrow \text{determine effective mass}$$

Cyclotron Resonance of Electrons and Holes in Silicon and Germanium Crystals

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(Received December 16, 1954)

Wannier-Mott Excitons

- Conduction band: electrons with mass m_e^*
- Valence band: holes with mass m_h^*
- Hydrogen problem with very light 'proton' in a screened environment

- Screening: $e^2 \rightarrow e^2 / \epsilon_r$

- Reduced mass: $m_e \rightarrow \mu = \left[\frac{1}{m_e} + \frac{1}{m_h} \right]^{-1}$

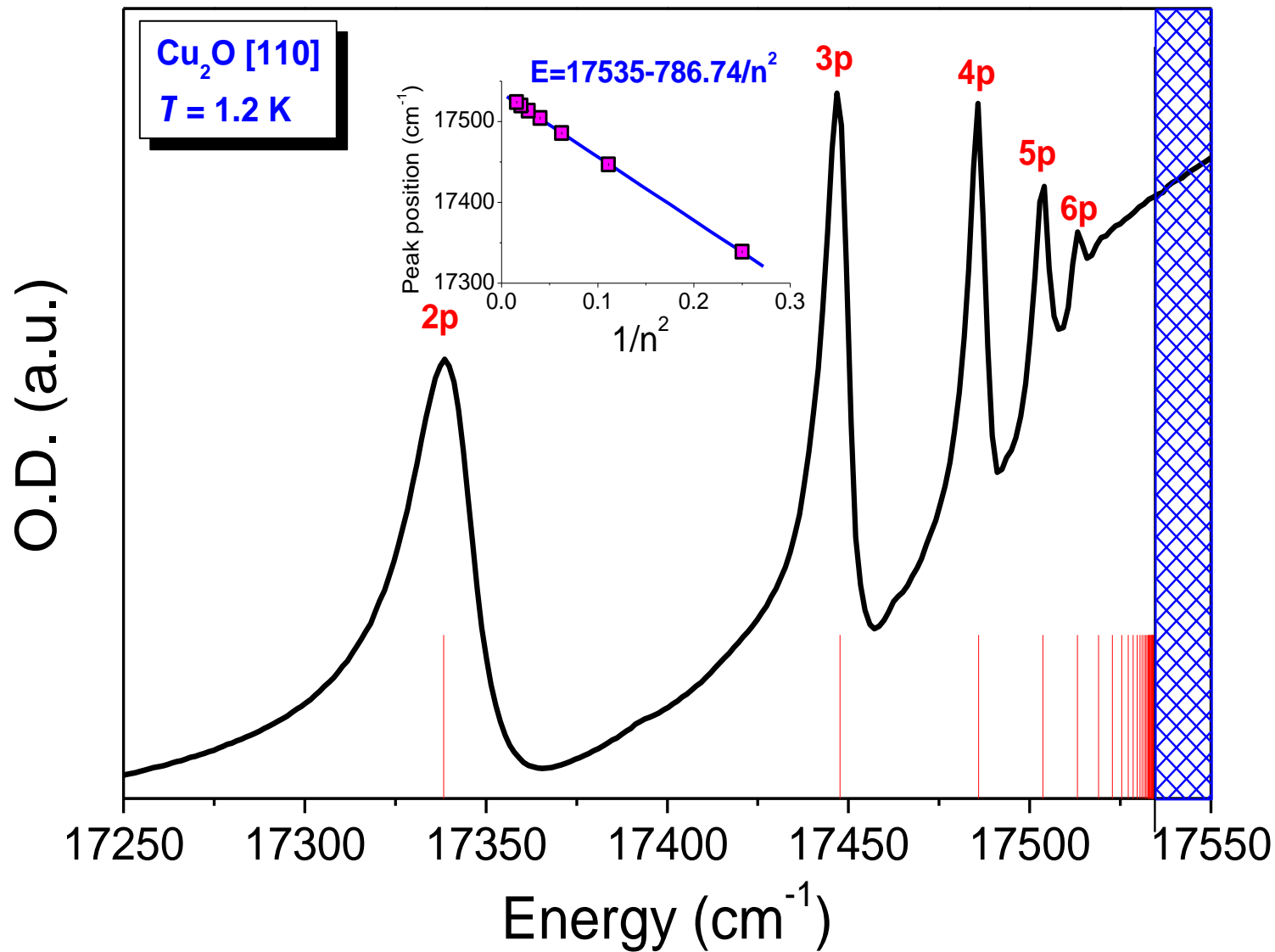
$$H = \frac{p_e^2}{2m_e} + \frac{p_p^2}{2m_p} - \frac{e^2}{|r_e - r_p|} \Rightarrow H = \frac{p_e^2}{2m_e^*} + \frac{p_h^2}{2m_h^*} - \frac{e^2}{\epsilon_r |r_e - r_h|}$$

$$a_{ex} / a_H = \frac{m_e}{\mu} \epsilon_r \approx 20$$

$$E_{ex} / E_H = \frac{\mu}{m_e} \frac{1}{\epsilon_r^2} \approx \frac{1}{144}$$

	Hydrogen	Cu ₂ O
Bohr radius	0.53 Å	10.6 Å
Binding E ₁	13.6 eV	94 meV

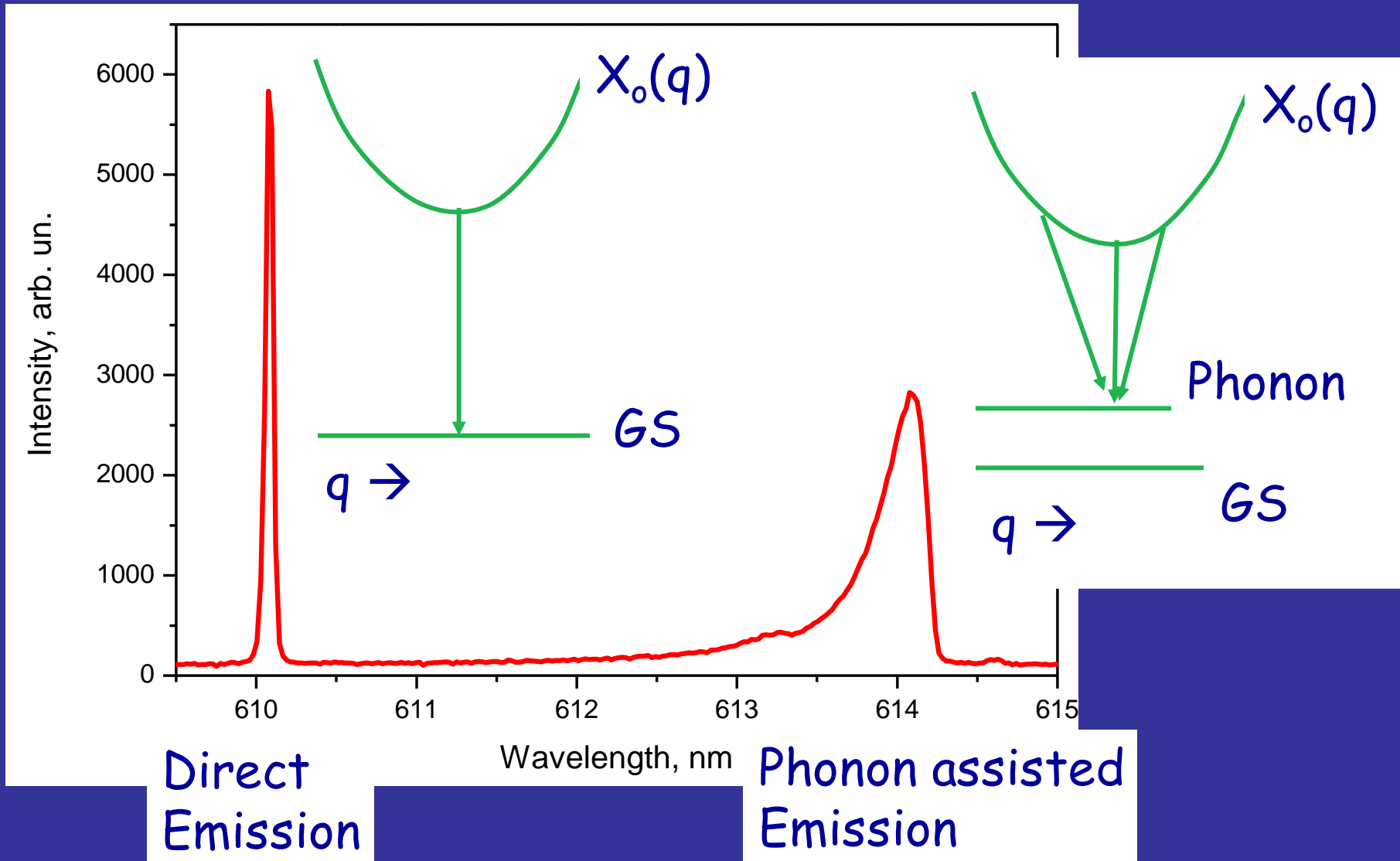
Excitons in Cu_2O (absorption)



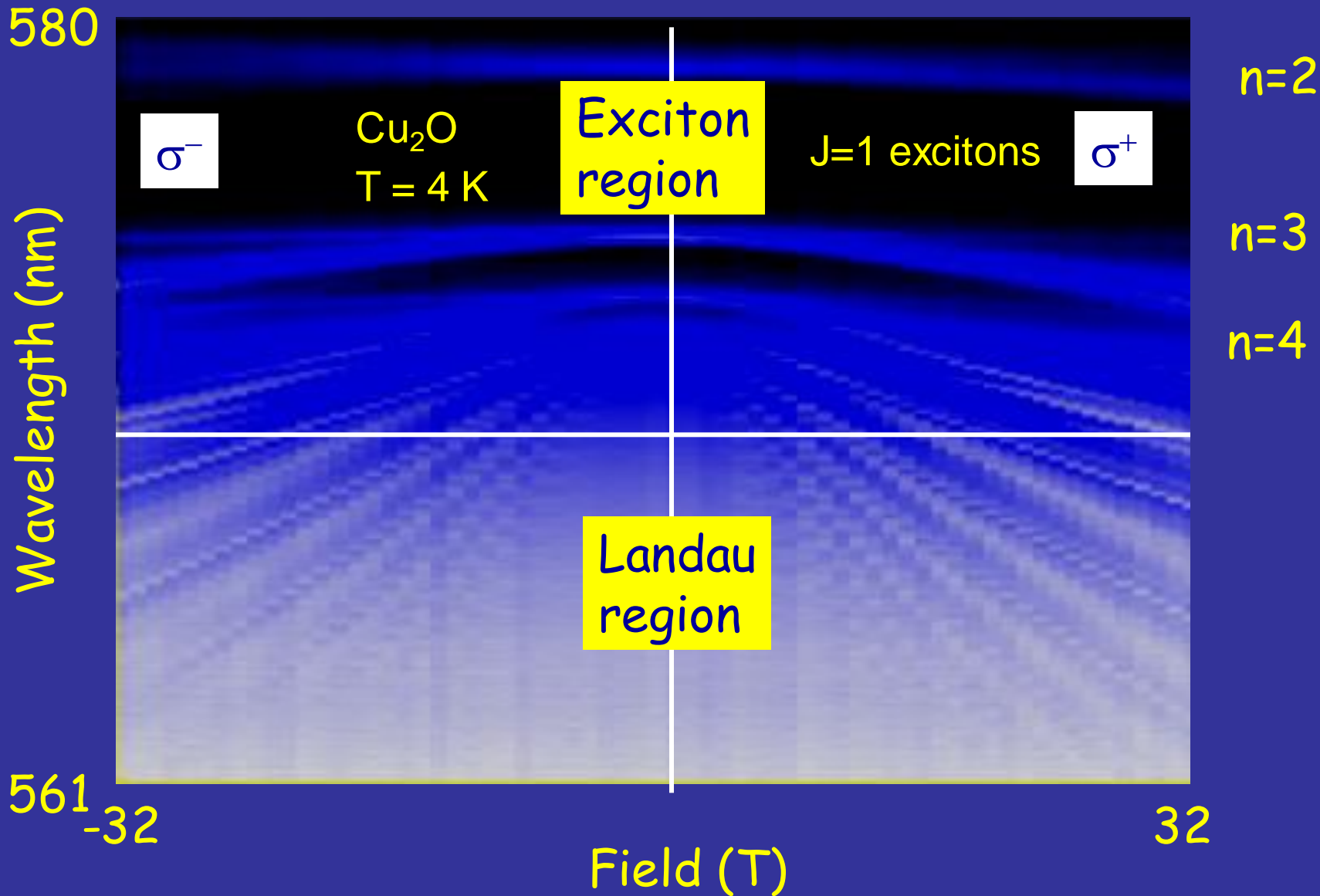
Lyman series

$$E(n) = \frac{E_0}{n^2}$$

Cu_2O Emission



Magneto-absorption of excitons



Excitons in KBr

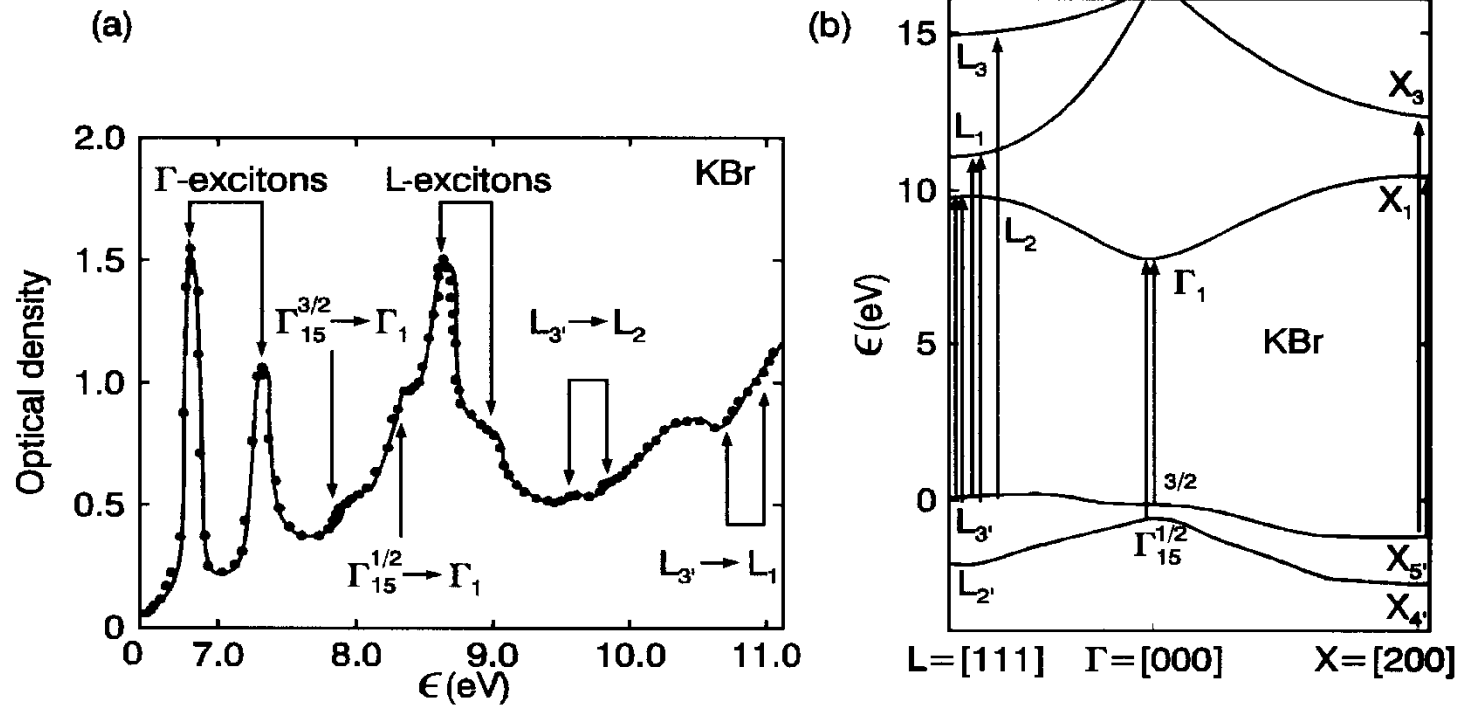


Fig. 7.7. Optical density for KBr measured at 80 K (a) and band structure for the corresponding lattice (b); after [7.11].

PHYSICAL REVIEW

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Ultraviolet Absorption of Alkali Halides*

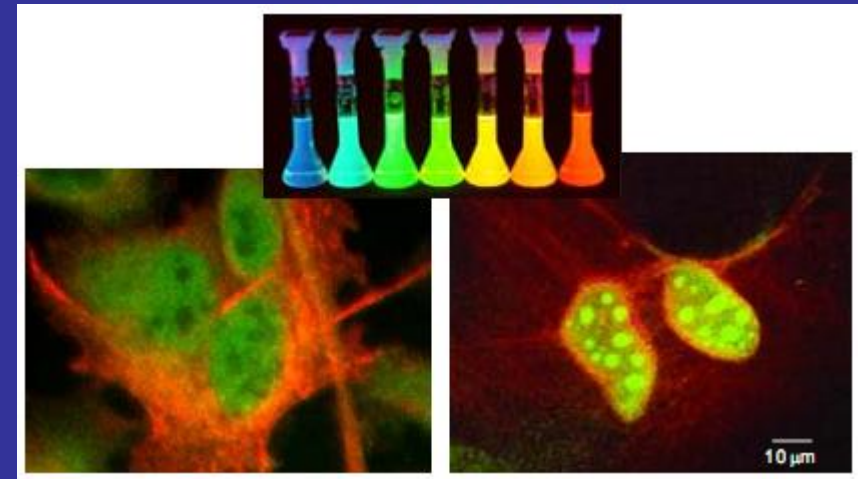
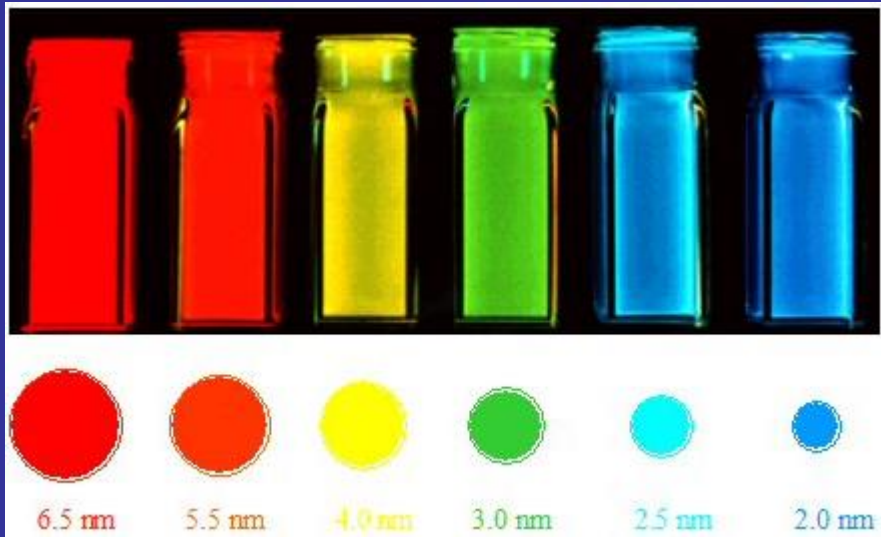
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(Received May 27, 1959; revised manuscript received August 19, 1959)

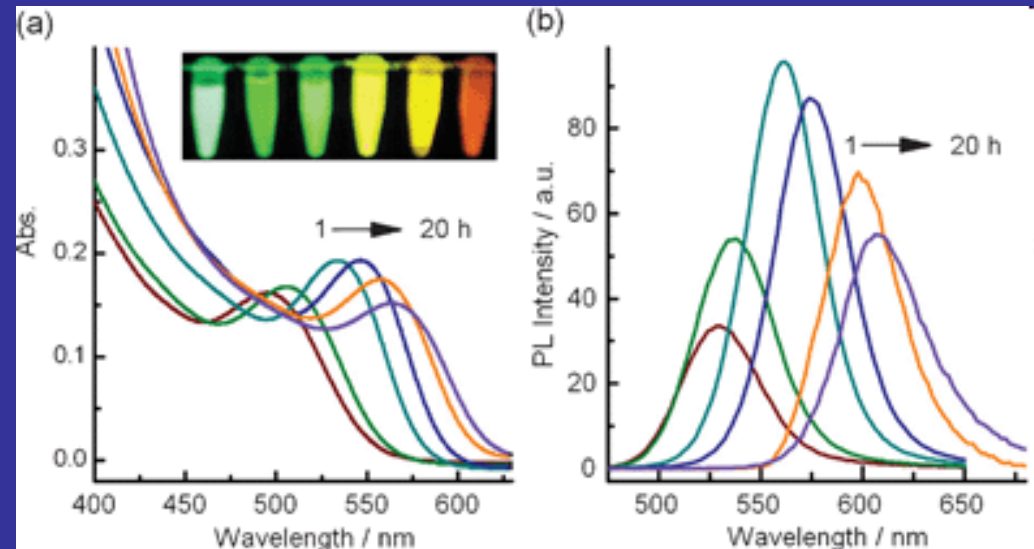
Nano Crystals

CdSe nanocrystals



CdTe nanocrystals

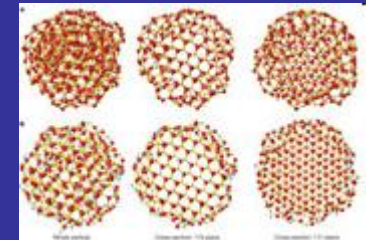
- Bio labeling
- Displays
- Solar cells
- Photonic crystals
- MRI enhancement
- ...



Nano Crystals

Bandgap CdTe: 1.56 eV (direct)

Bulk \rightarrow emission at 795 nm



Small particle: confinement energy (particle in a box)

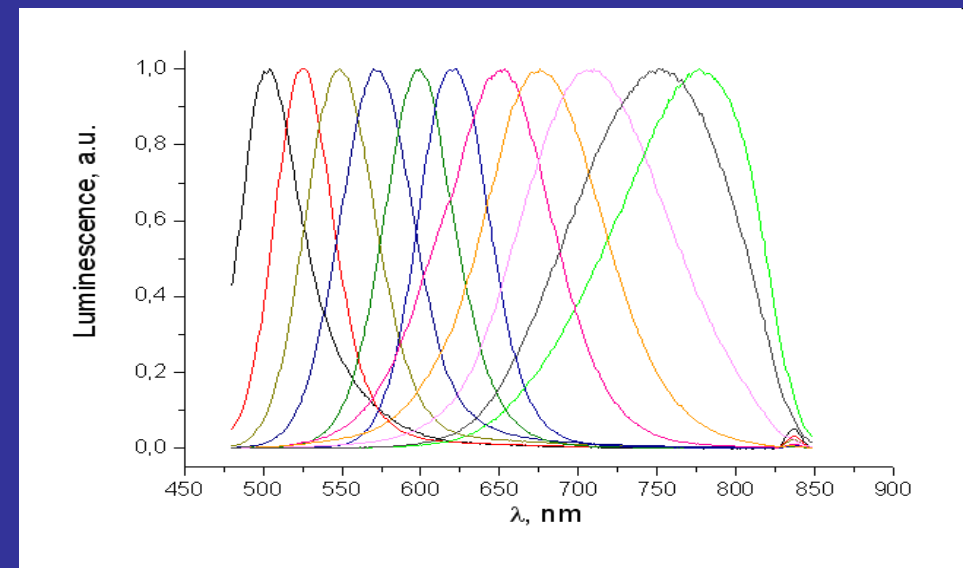
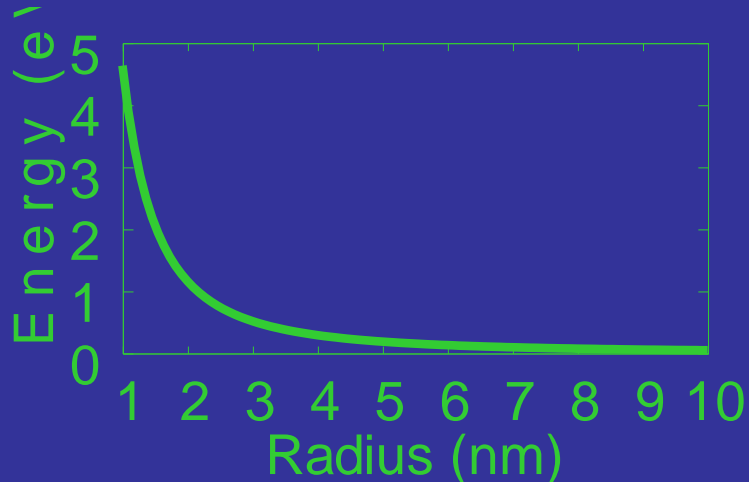
$$E = E_g + \frac{\hbar^2 \pi^2}{2\mu R^2}$$

$$\left. \begin{array}{l} \text{CdTe: } m_e^* \approx 0.1 m_0 \\ m_h^* \approx 0.44 m_0 \end{array} \right\} \mu \approx 0.08 m_0$$

2 nm particles: Confinement 1.15 eV

$E = 1.56 + 1.15 = 2.71$ eV Corresponds to 475 nm

For 3 nm: 600 nm



Exercises

- Derive the wave equation
- 1.8; 1.12; 1.19
- Derive the response function of a Lorentz oscillator
- 2.3; 2.6;
- 3.13
- 6.3, 6.18
- 7.1, 7.6, 7.7